

# Parameterizing vertical mixing in global ocean models: progress and challenges

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GDR Défis théoriques pour le climat, 2023

# REVIEWS

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# The polar ocean and glacial cycles in atmospheric CO<sub>2</sub> concentration

Daniel M. Sigman<sup>1</sup>, Mathis P. Hain<sup>1,2</sup> & Gerald H. Haug<sup>2,3</sup>

**“In defence of the stratification hypothesis, the models’ calculation of mixing between different density waters in the ocean interior is highly suspect, and yet this mixing is central to the models’ tendency for inverse behaviour between North Atlantic and Antarctic overturning.**

**The models can have too much deep mixing, and they generally do not take into account the fact that more energy is required to mix across a greater density difference.**

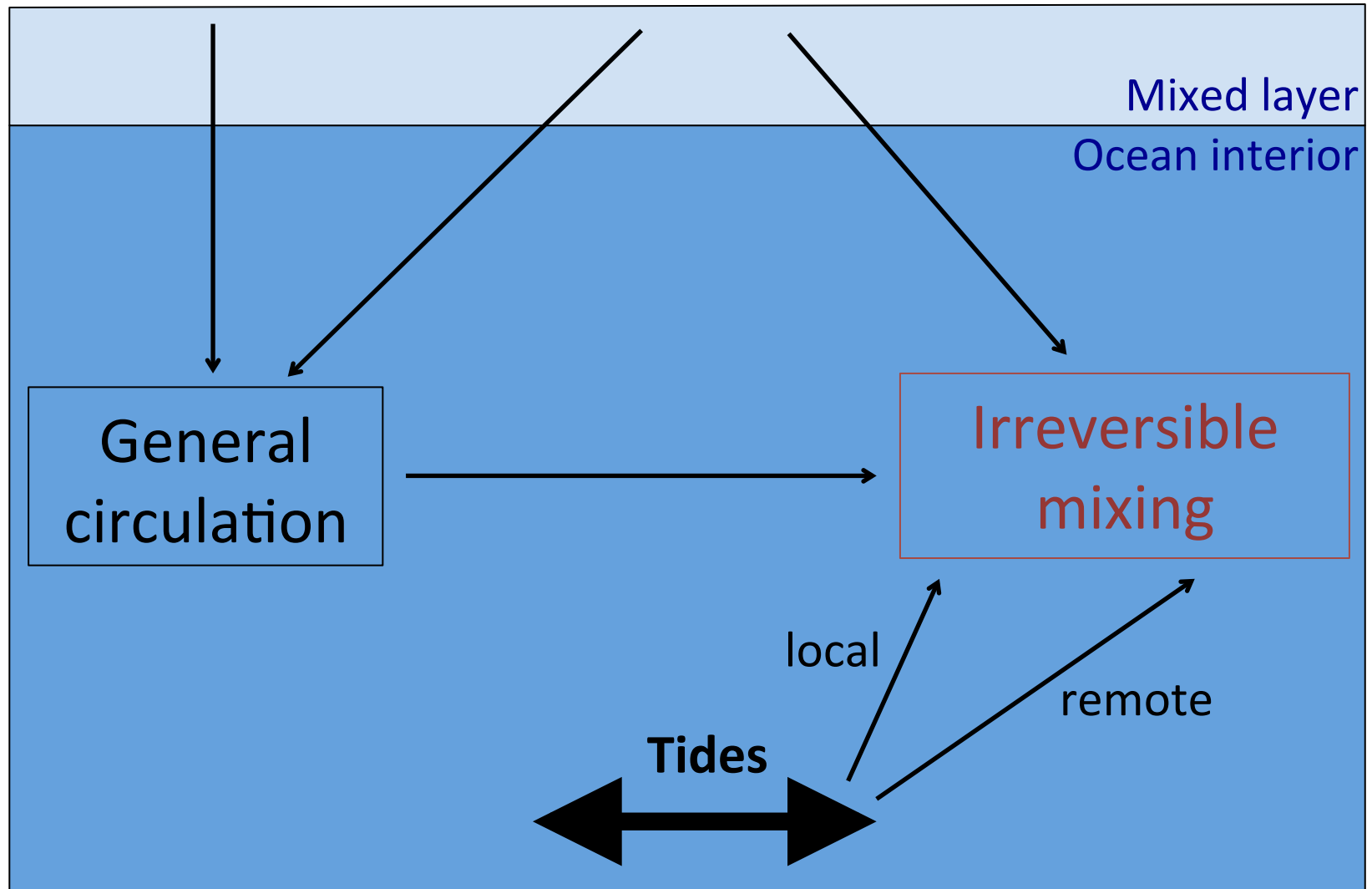
**Deep mixing may be the Achilles’ heel of the models that has prevented them from capturing a climate change that greatly decreases the global demand for new deep water.”**

# Energy flows from forcing to dissipation

Surface buoyancy fluxes



Winds

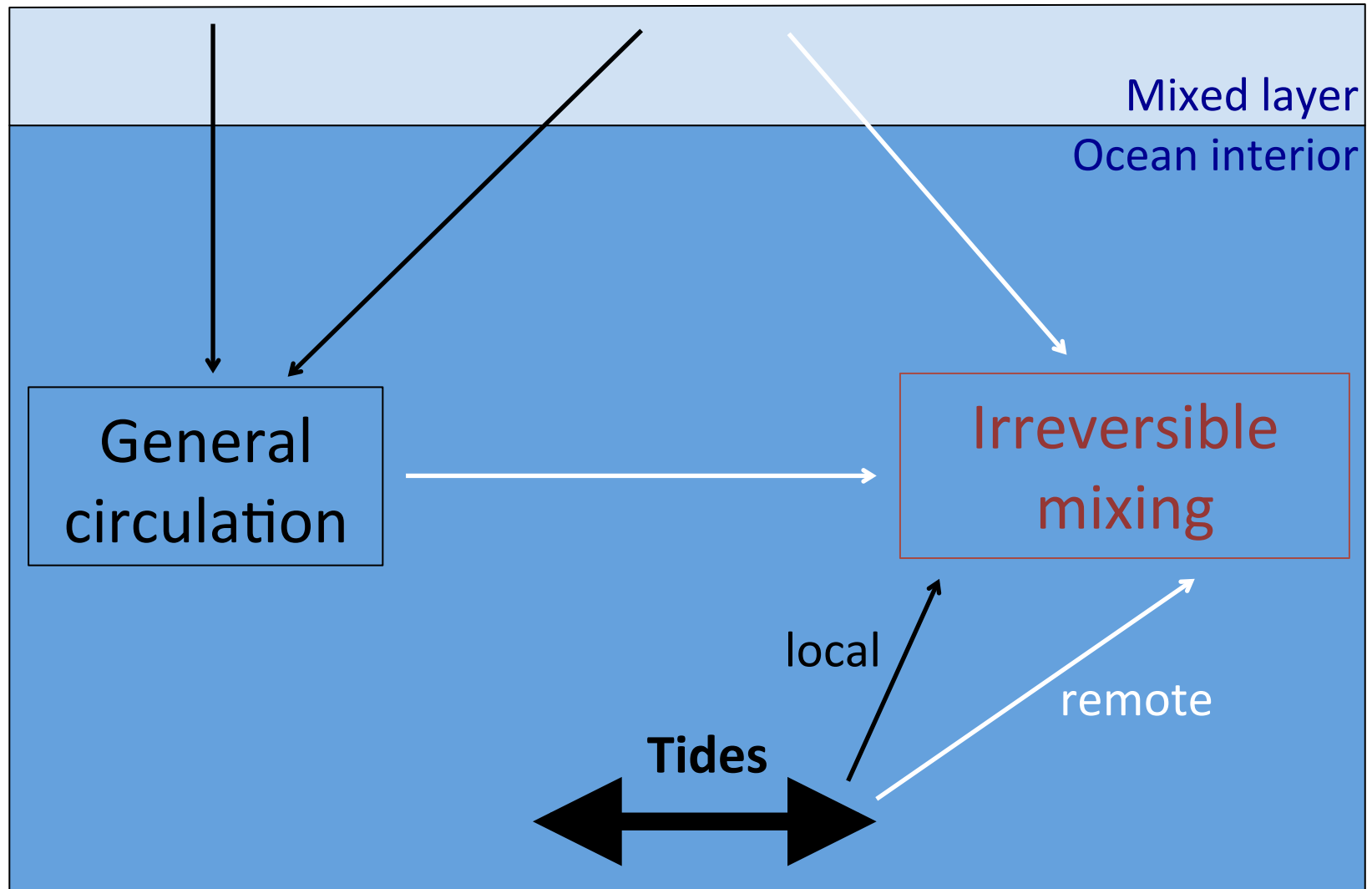


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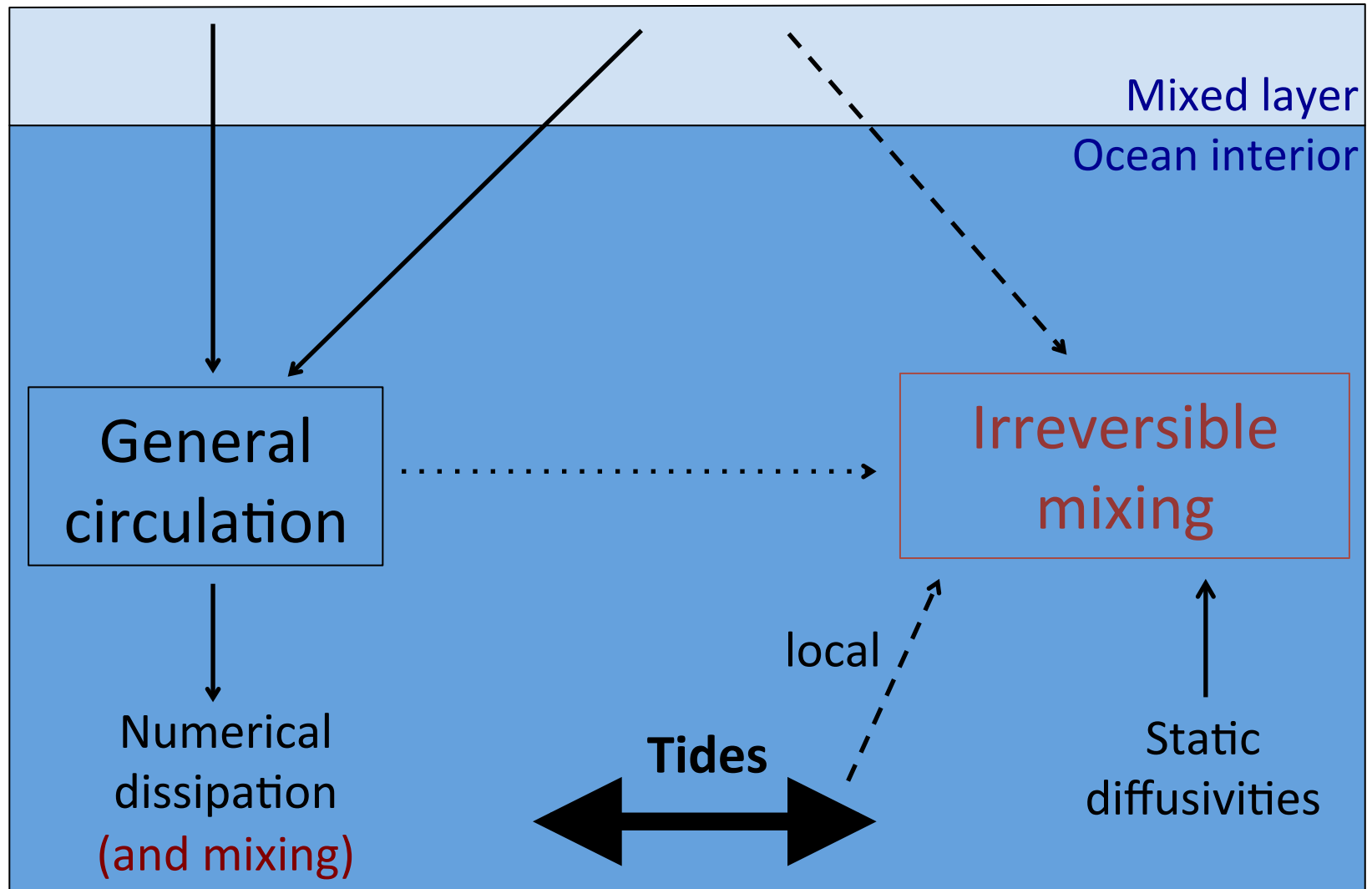


# Energy flows in ocean models

Surface buoyancy fluxes



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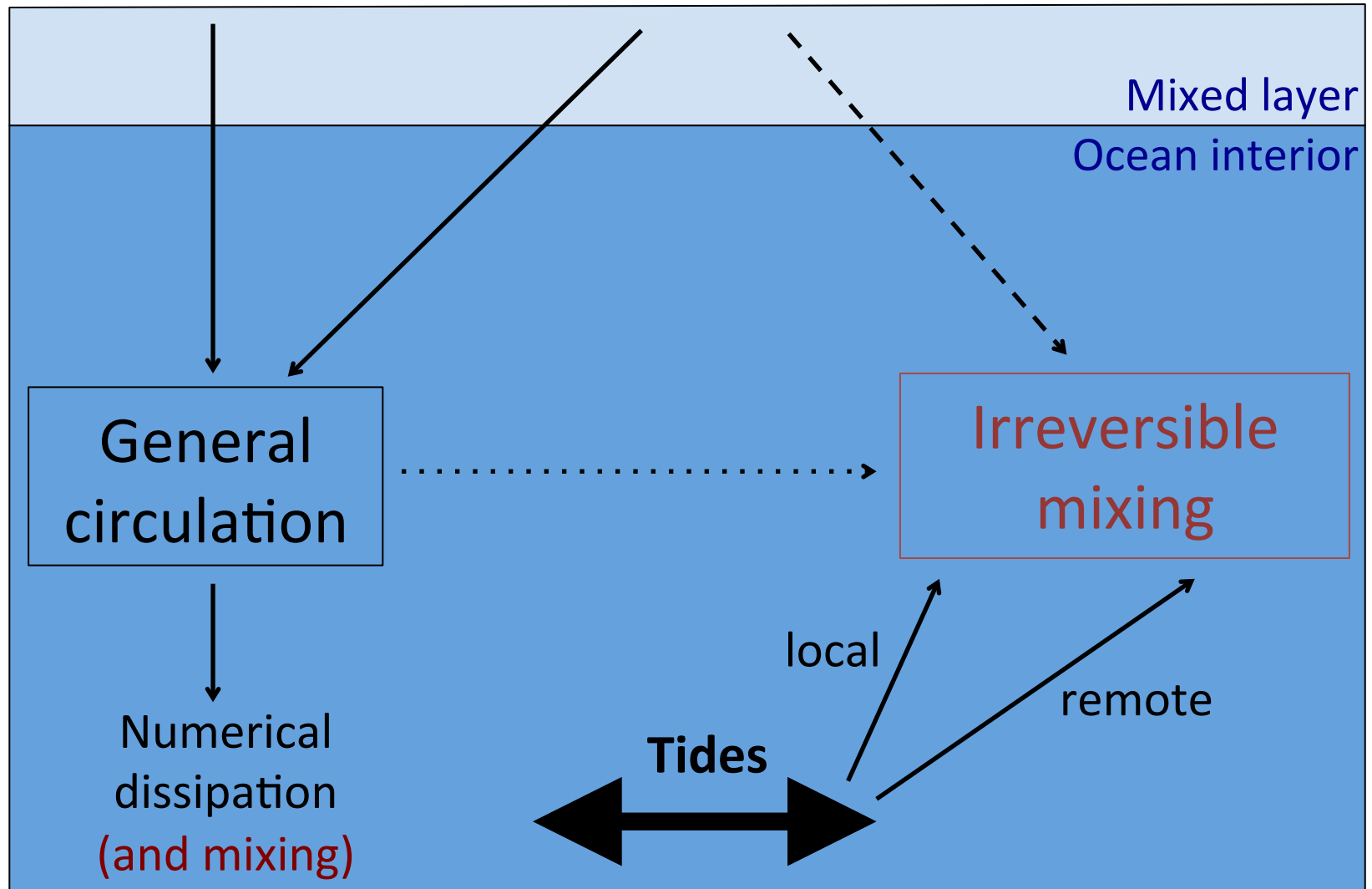


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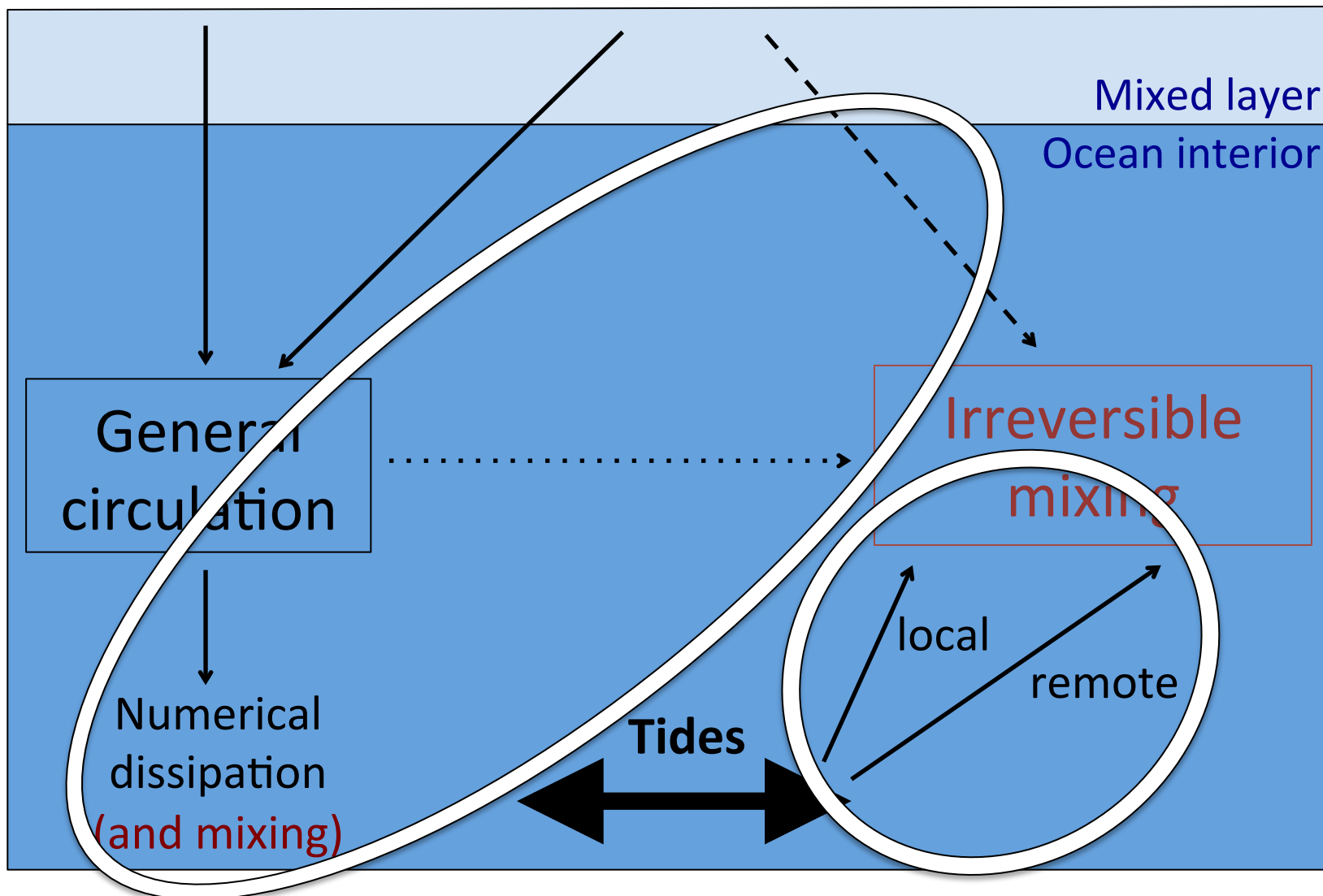


# Energy flows in ocean models

Surface buoyancy fluxes



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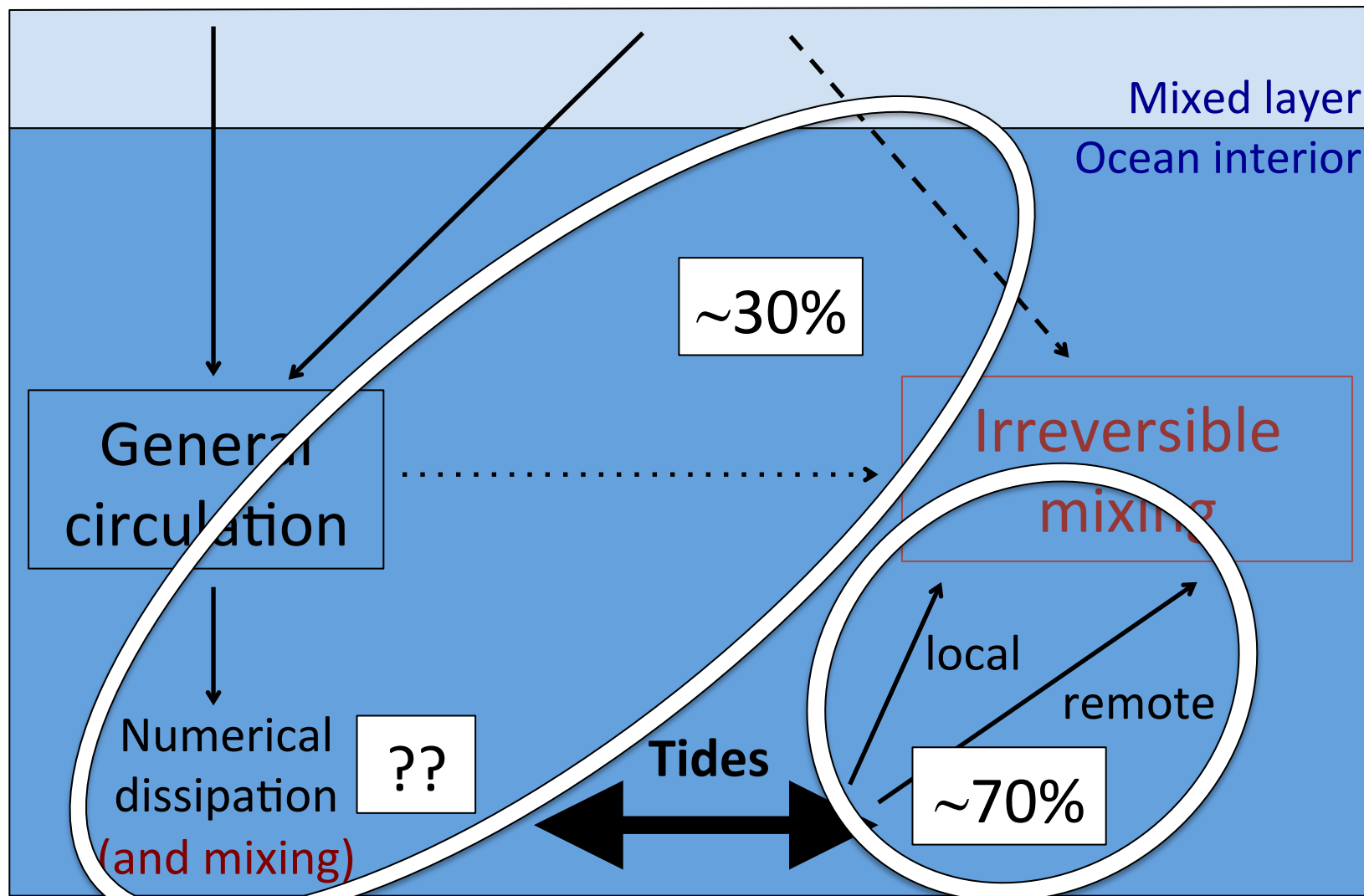


# Energy flows in ocean models

Surface buoyancy fluxes



Winds



# Outline

## **1. Progress: new tidal mixing schemes**

- Rationale
- Impact in global ocean simulation
- Comparison to mixing observations

## **2. Challenges:**

- Wind-induced inertial oscillations
- Submesoscale instabilities
- Numerical mixing

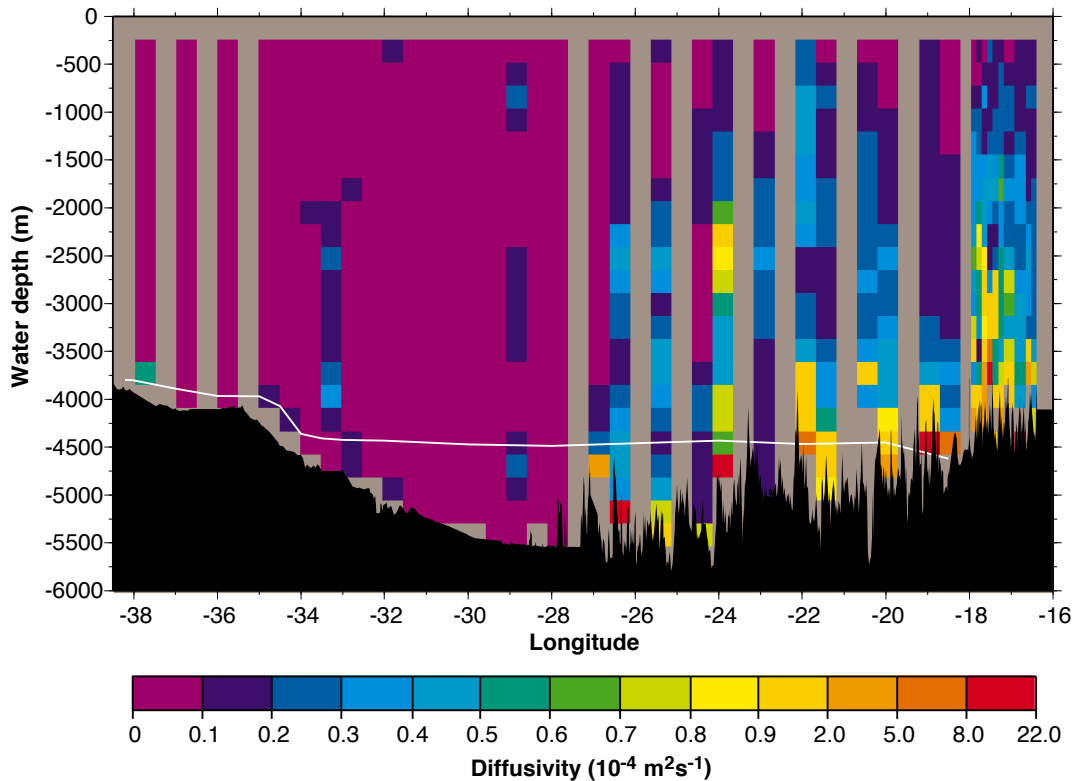
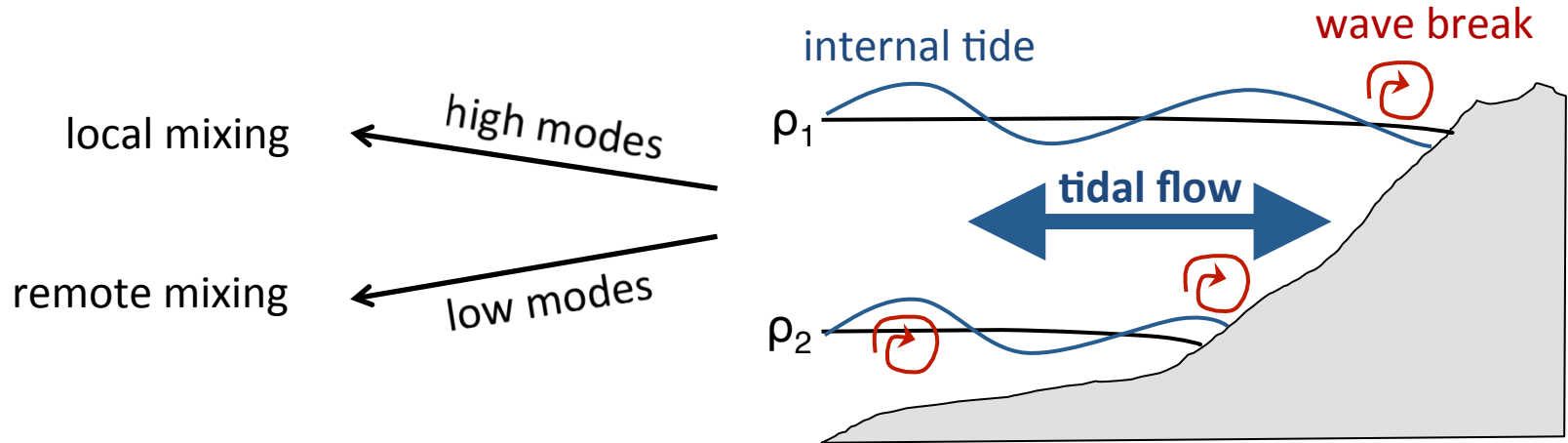
# **1. Progress: new tidal mixing schemes**

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# Local and remote tidal mixing



Depth-longitude transect of turbulent diffusivity across the Brazil Basin.

From Polzin et al. (1997).

# Old practice in global ocean models

- Remote: tuneable background  $K_z$  ( $\approx 10^{-5} \text{ m}^2\text{s}^{-1}$ ).
  - Independent of ocean state.
  - No control on (evolving) energy required to maintain such background mixing.
- Local: bottom-intensified mixing energy.
  - 2D map of locally-dissipating internal tide energy ( $qE$ ).
  - Fixed (exponential) vertical energy structure ( $F$ ).

$$K_z = 0.2 qE F / \rho N^2$$

# New schemes

- No background diffusivity.
- All mixing comes from known energy sources.
  - Read static 2D maps of power input to internal tides.
  - Redistribute this power within simulated stratification.
  - Deduce  $K_z$  from local dissipation  $\varepsilon$  via a standard turbulent closure (e.g. zero order,  $K_z = R_f \varepsilon / N^2$ ).

# Online vs offline strategy

Internal tide  
lifecycle stage

Eden and Olbers  
2014

de Lavergne et al.  
2020

GENERATION

offline

offline

PROPAGATION

online

offline

2D DISSIPATION

online

offline

3D DISSIPATION

online

online

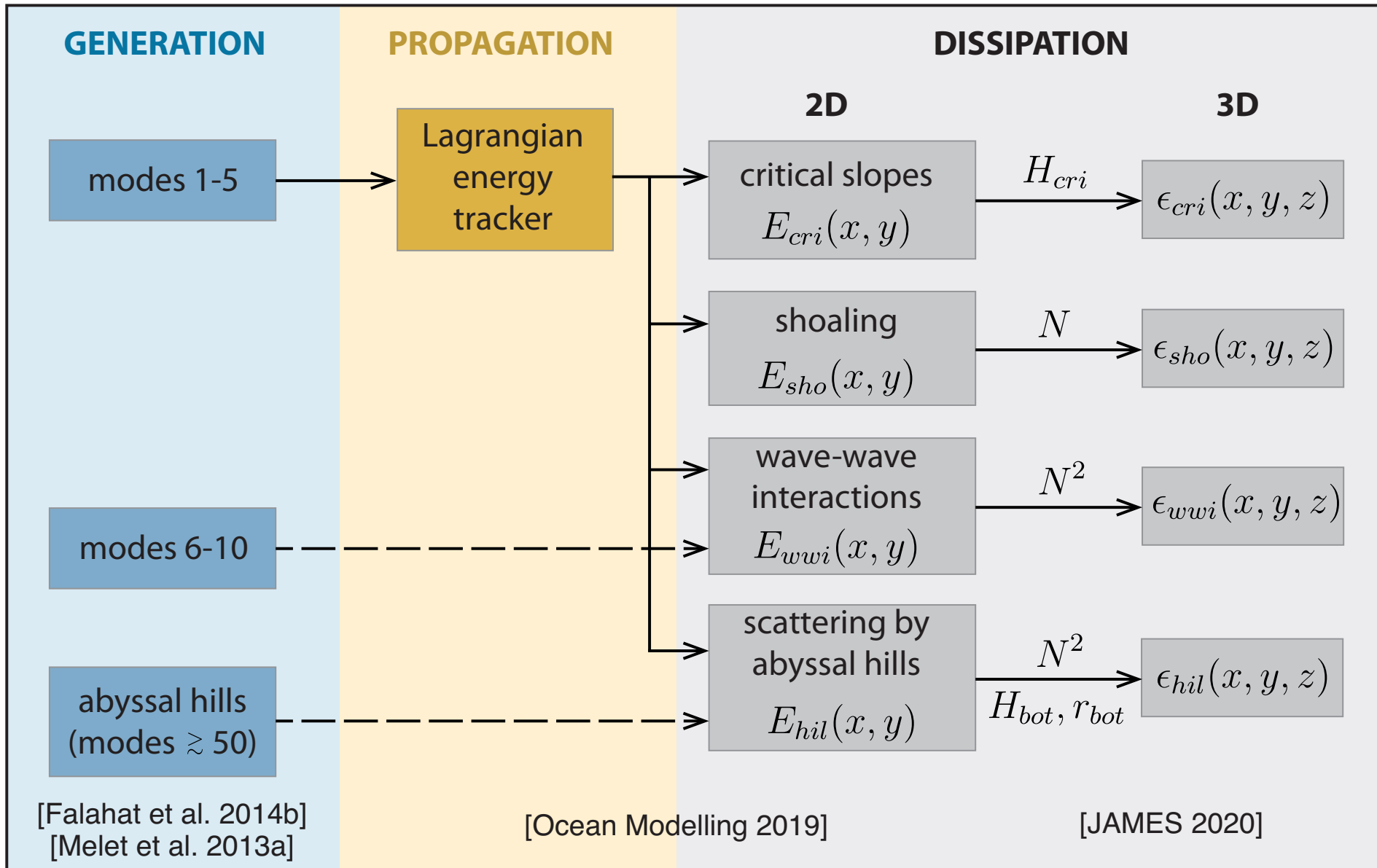
**interactivity**

**vs**

**accuracy**

# Methodology (de Lavergne et al. 2020)

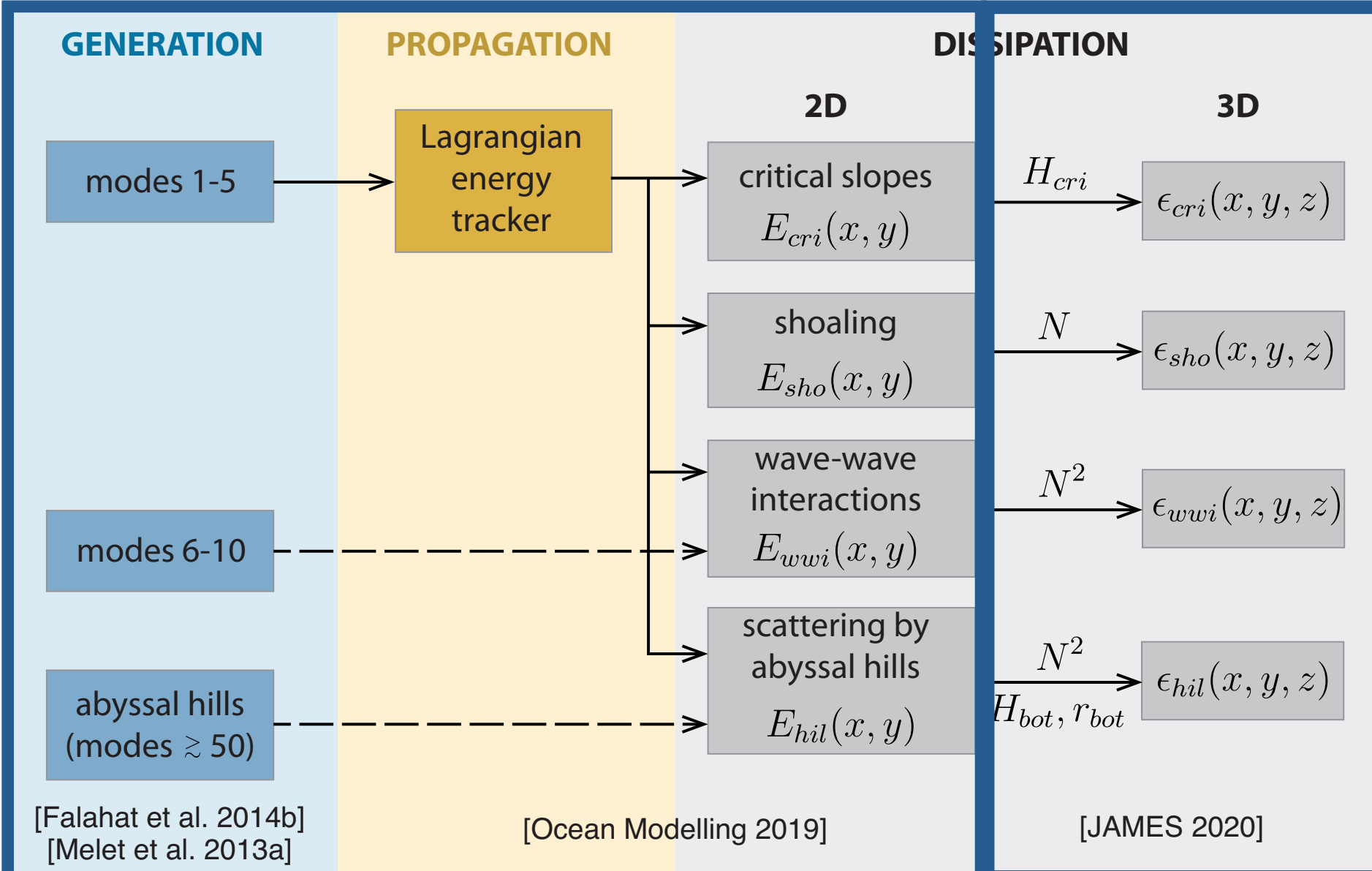
Mode-by-mode tracking of energy from sources to sinks





# Methodology (de Lavergne et al. 2020)

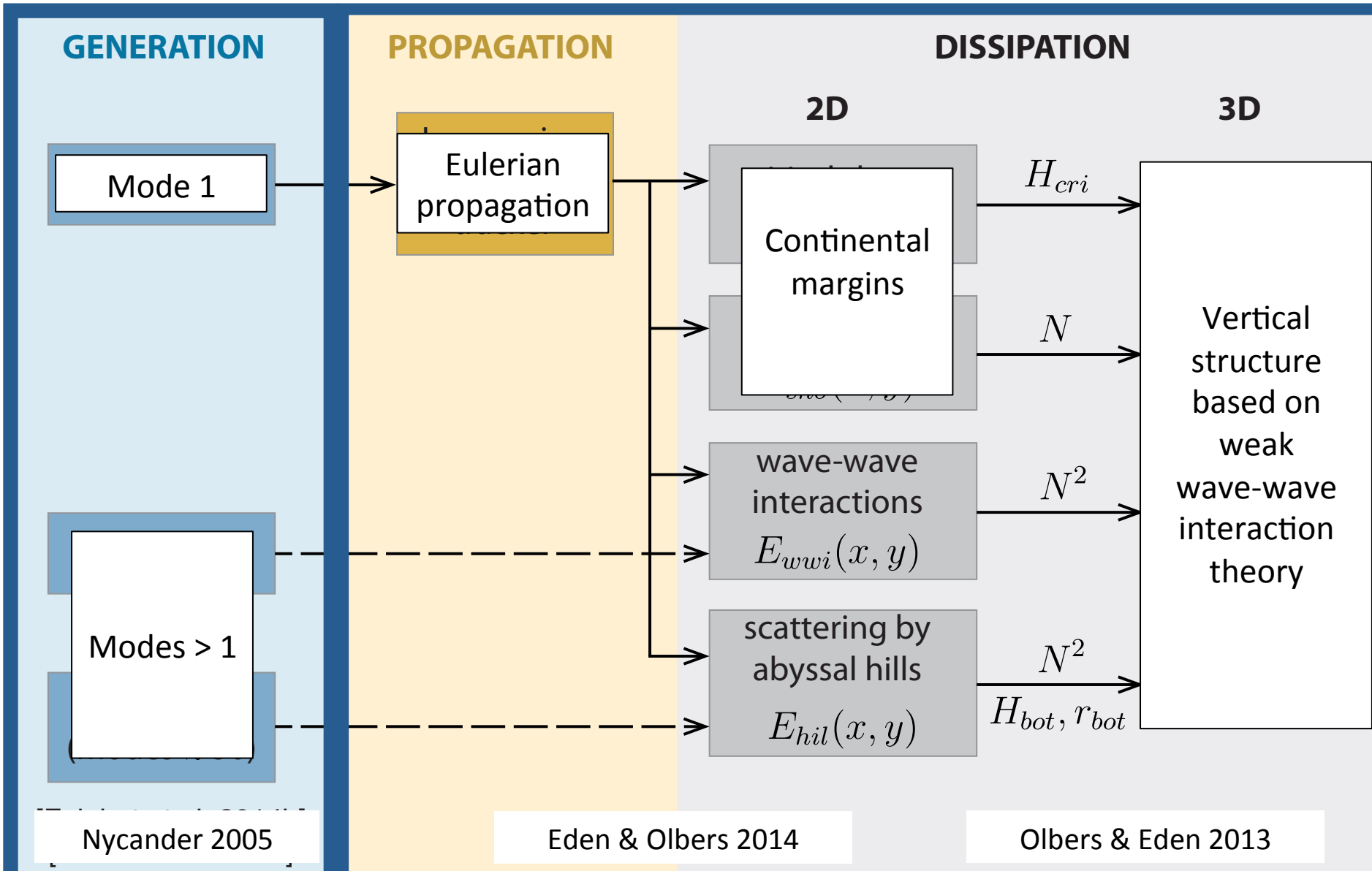
Static 2D maps of depth-integrated dissipation      Vertical structures



# Methodology (Eden and Olbers 2014)

Static 2D maps

Online energy redistribution



# Tracking low modes from sources to sinks

Evolution equation for a given mode's column-integrated energy  $E(t,x,y,\phi)$ :

$$\partial_t E + \mathbf{div}_{\vec{r},\phi} \vec{F} = G - D$$

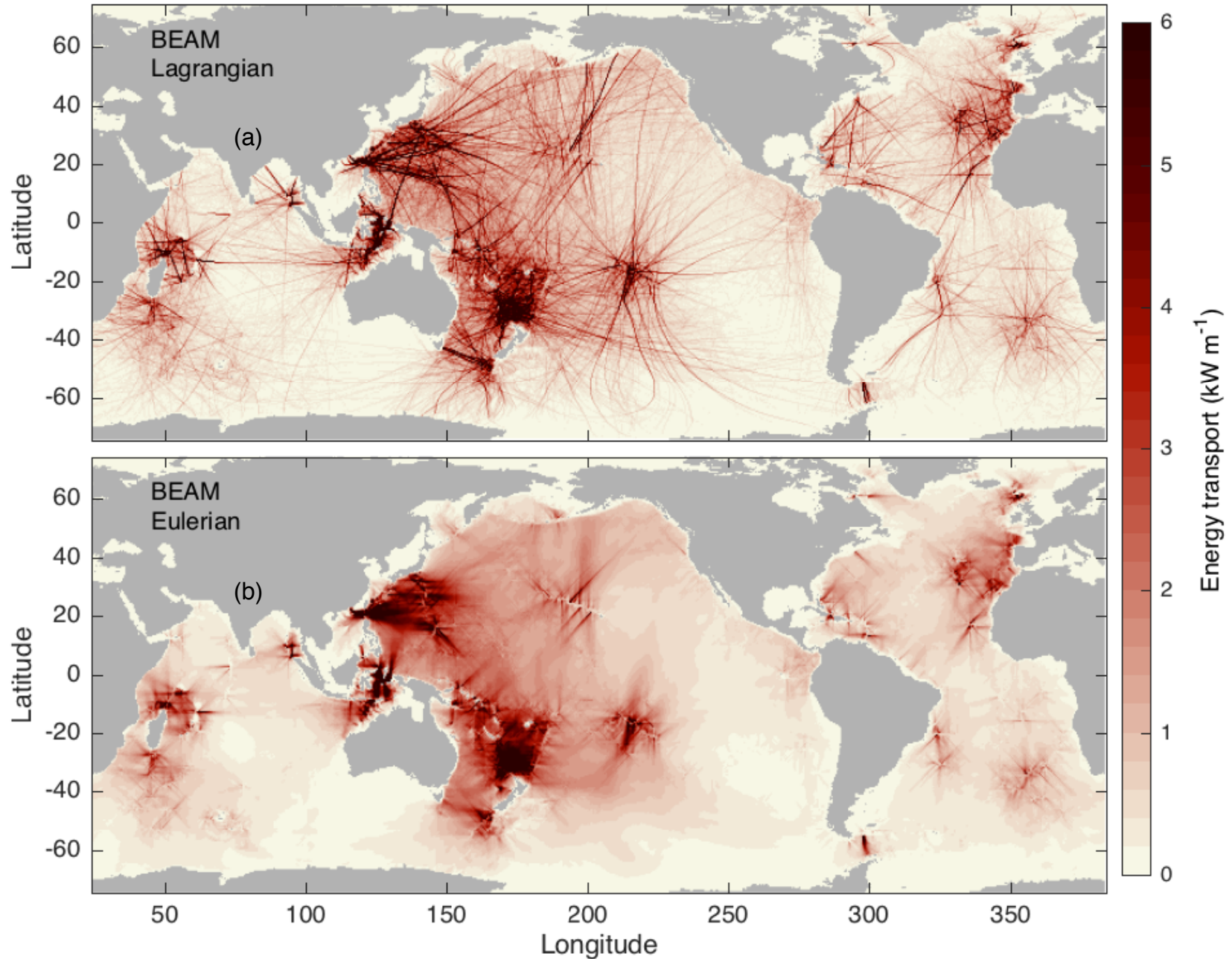
$D$ : energy sinks.

$G$ : angle- and position-dependent generation rate of considered mode.

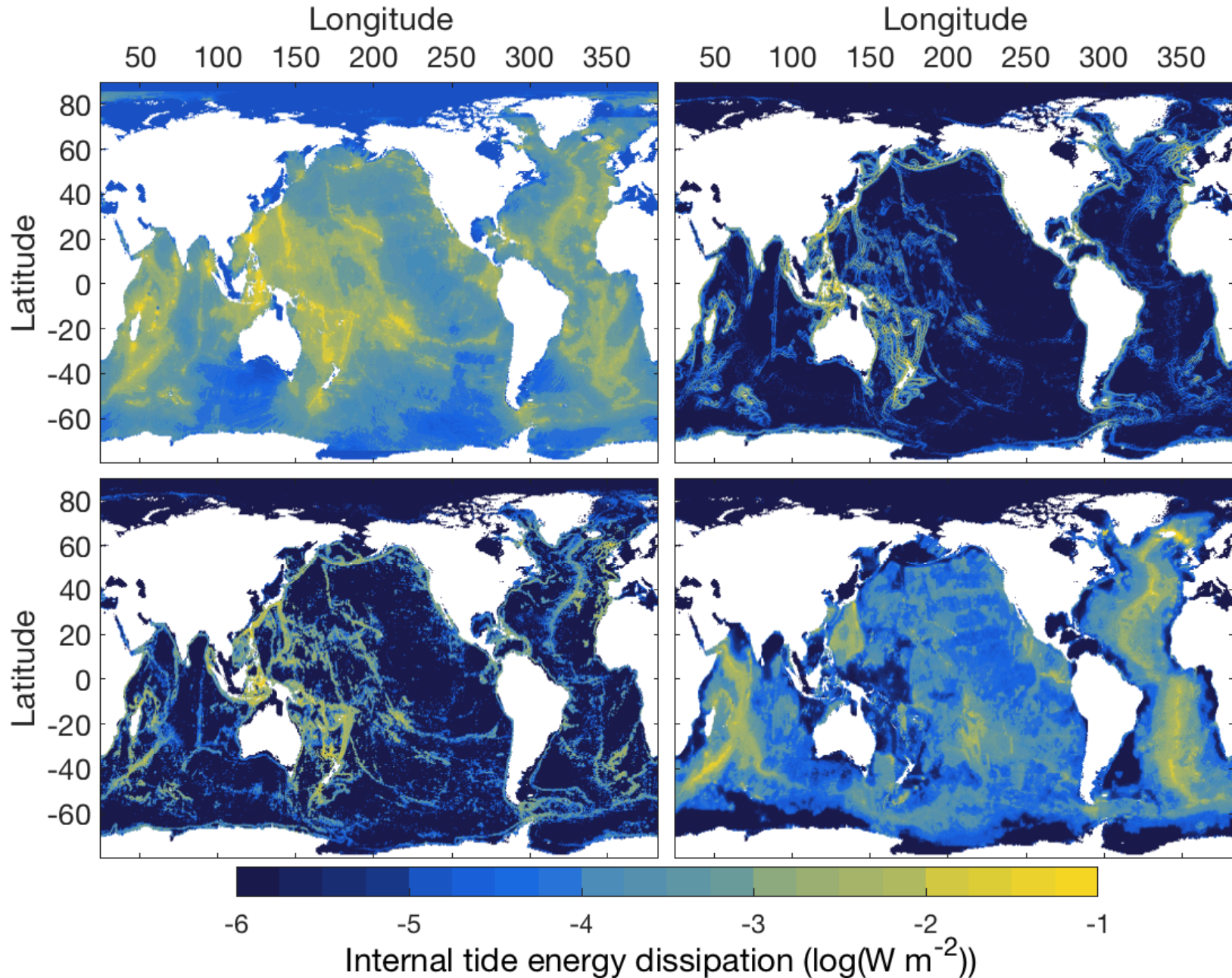
$F$ : horizontal energy transport by modal group velocity:  $\vec{F} = \vec{c}_g E$

- 60 maps:            5 vertical modes (1 to 5)
  - x 3 tidal constituents ( $M_2$ ,  $S_2$  and  $K_1$ )
  - x 4 dissipative processes.

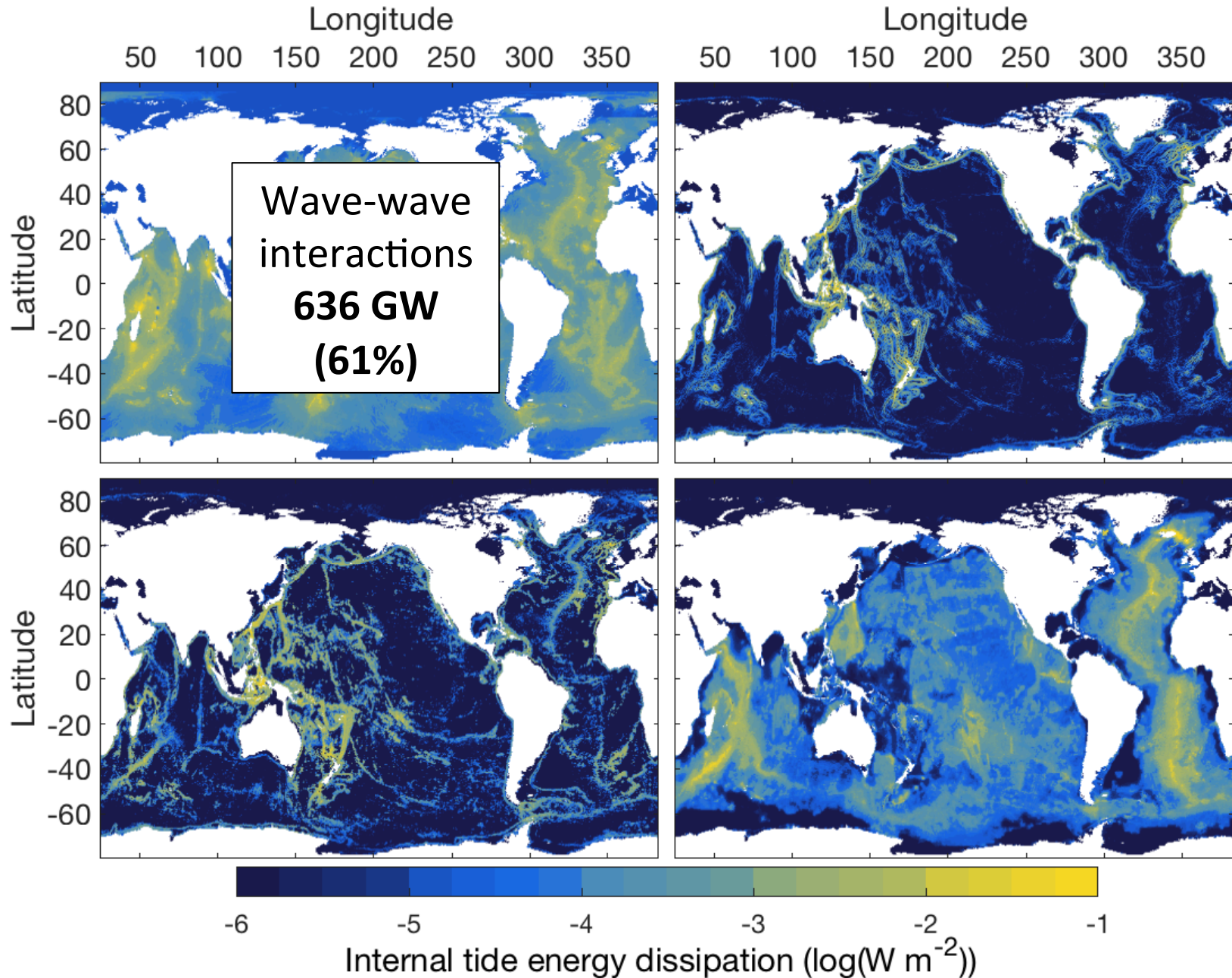
# Lagrangian versus Eulerian scheme



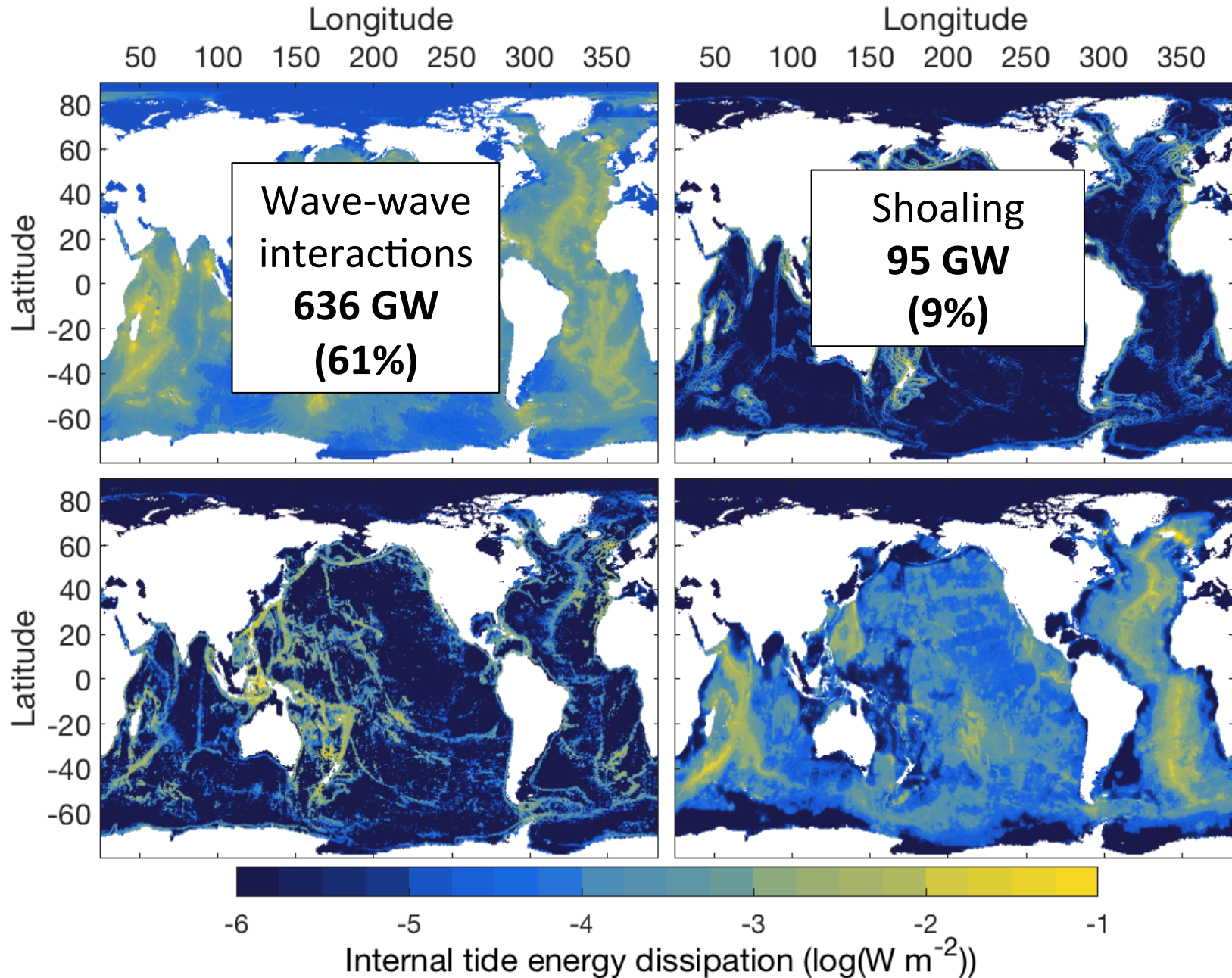
# 4 static maps...



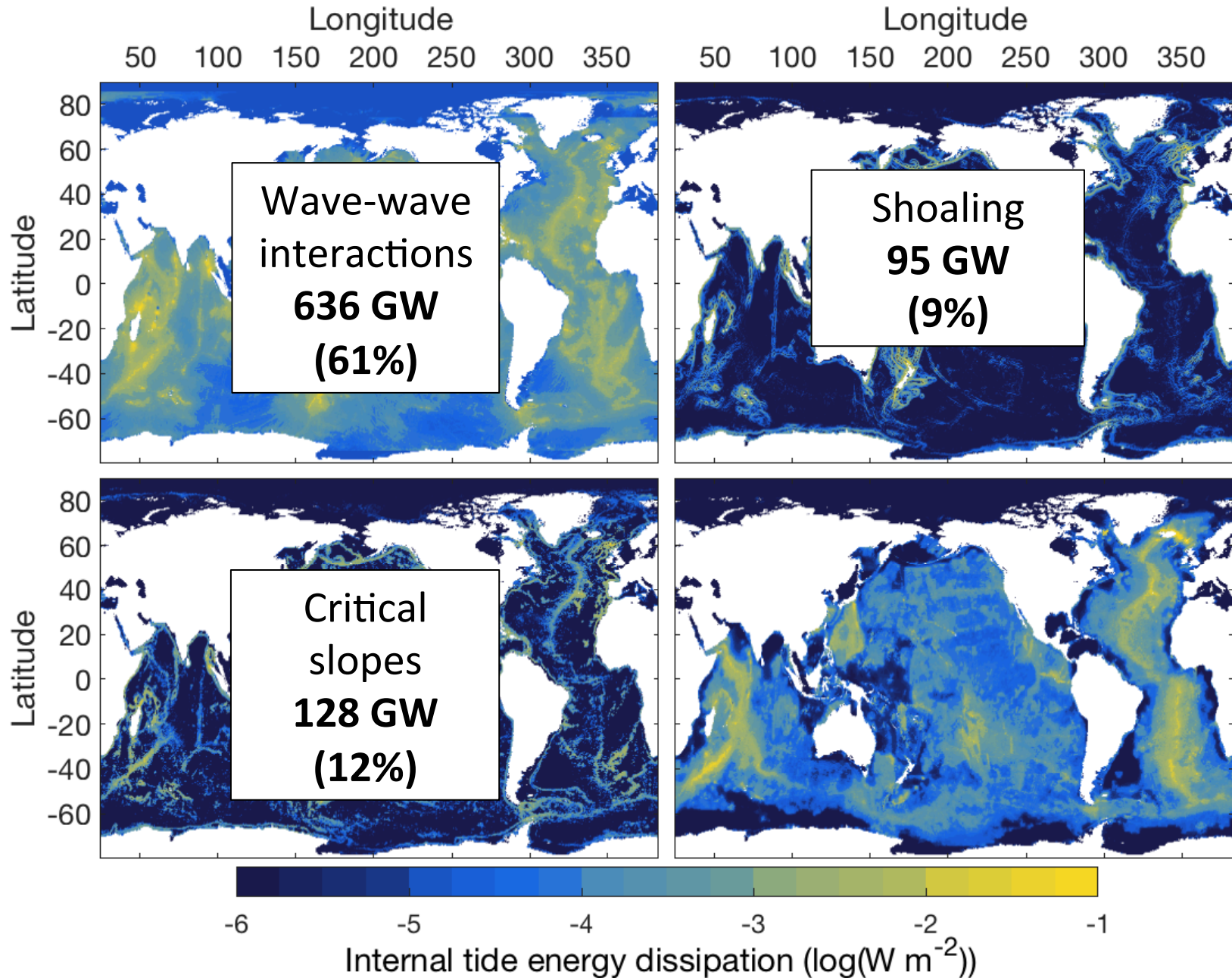
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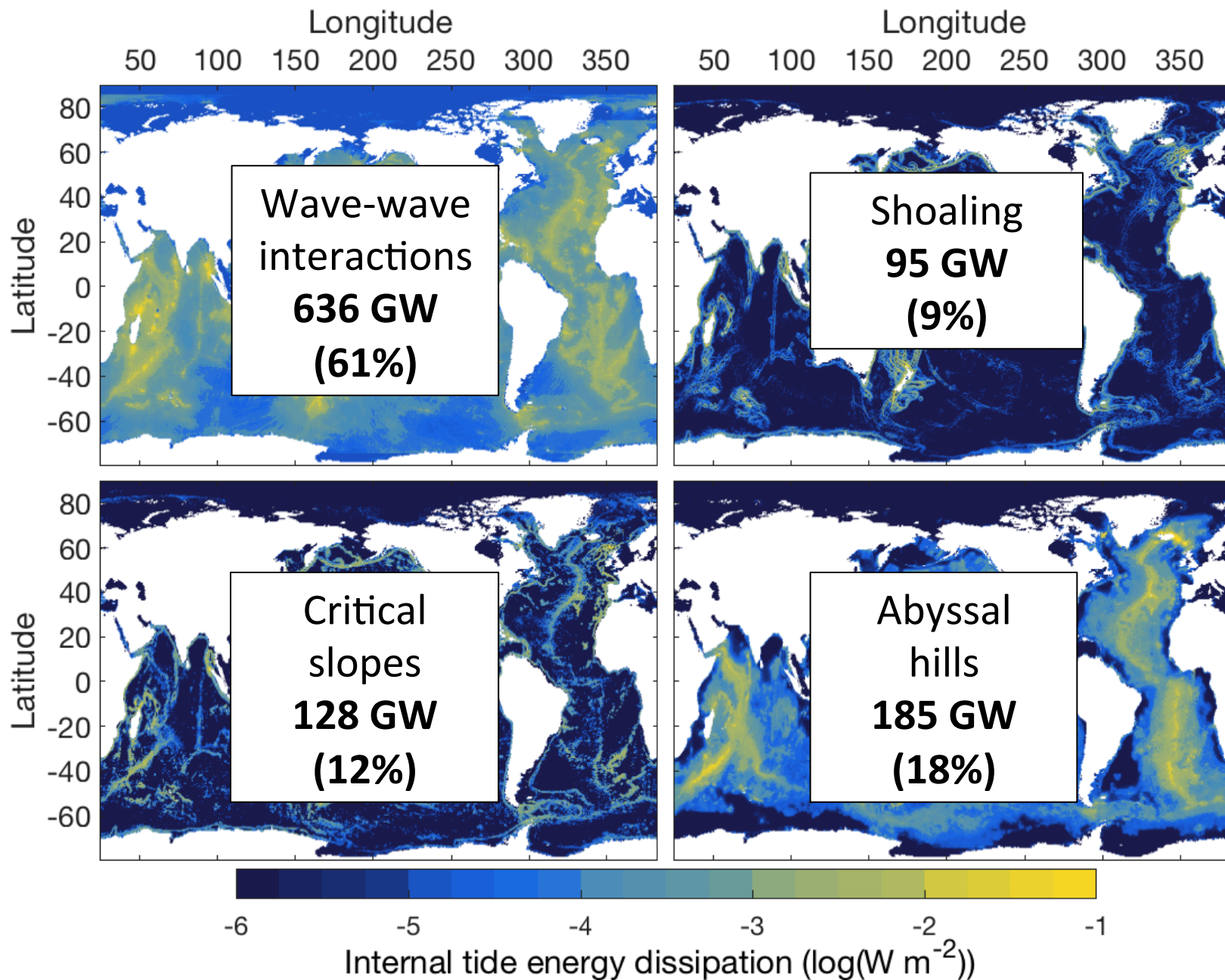


# 4 static maps...

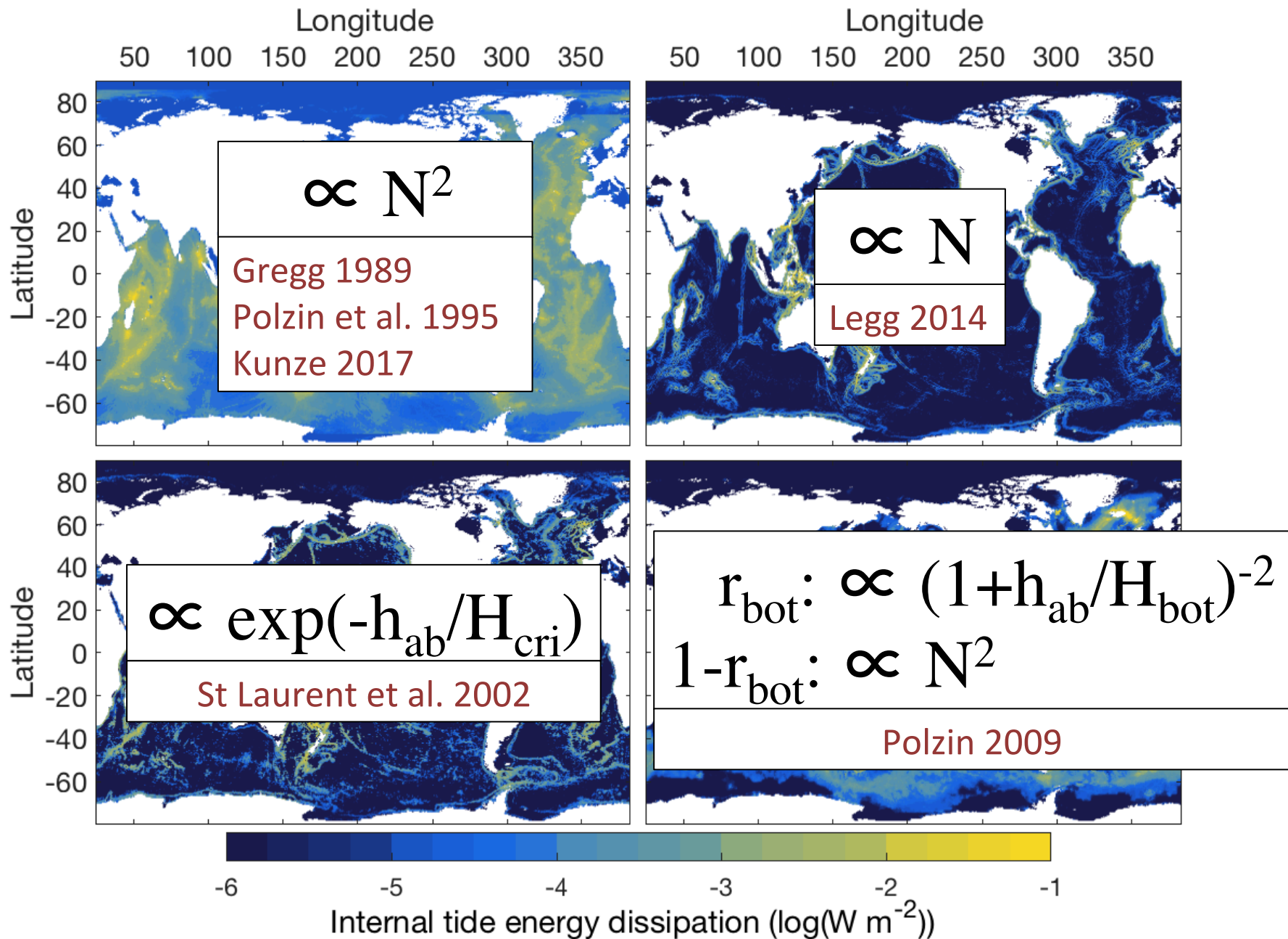




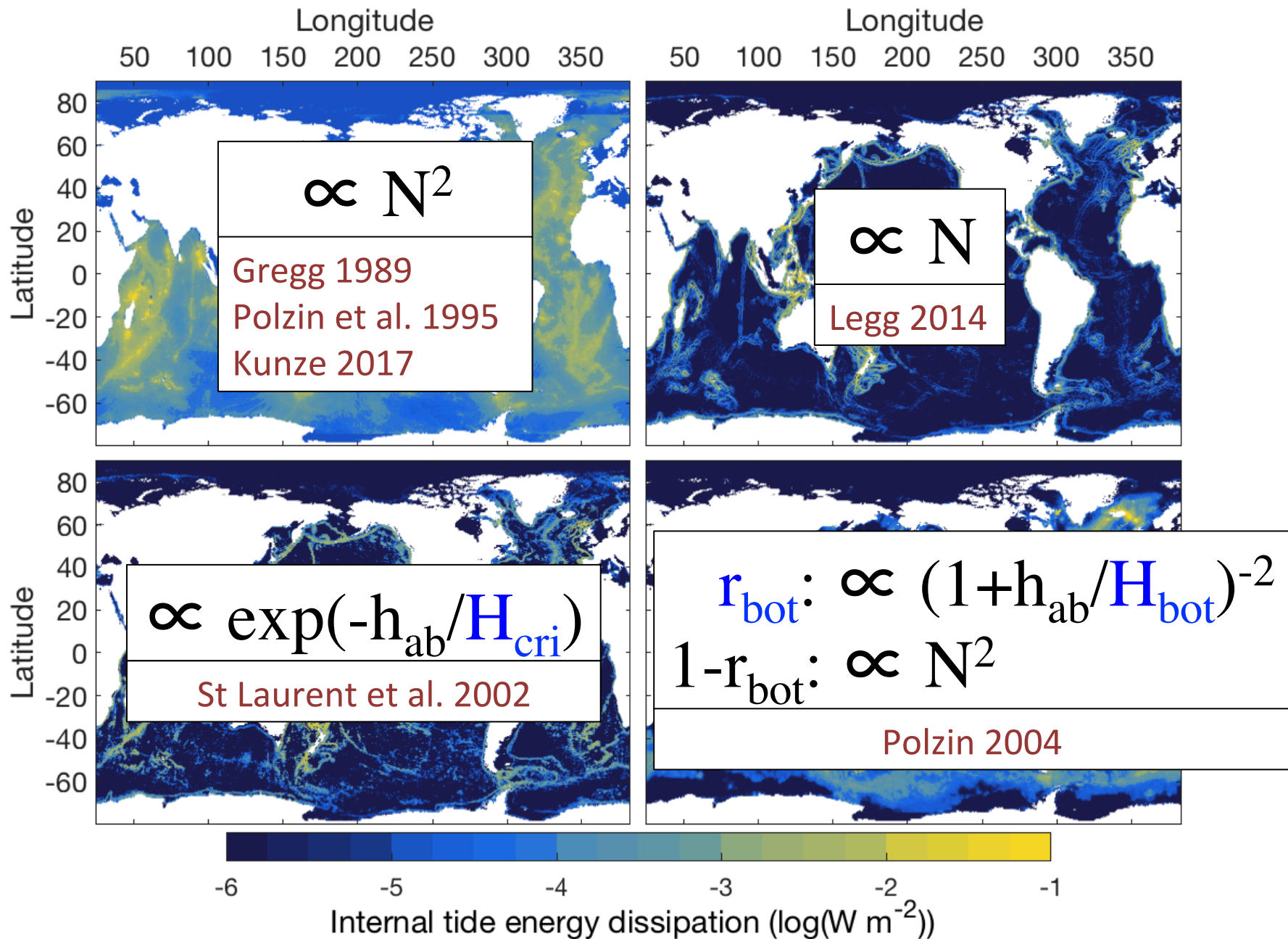
# 4 static maps...



# ...and 4 vertical structures



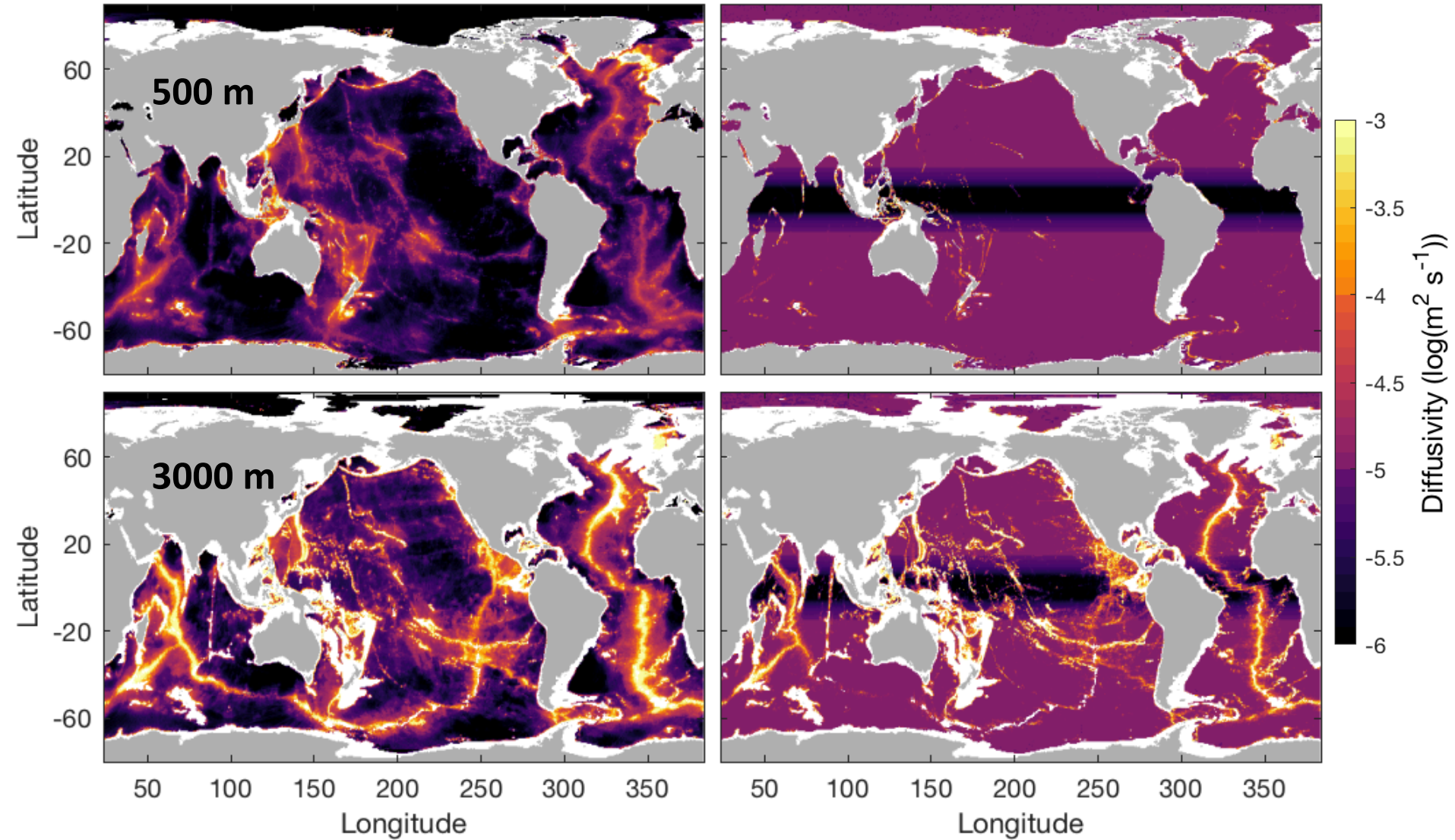
# ...and 4 vertical structures



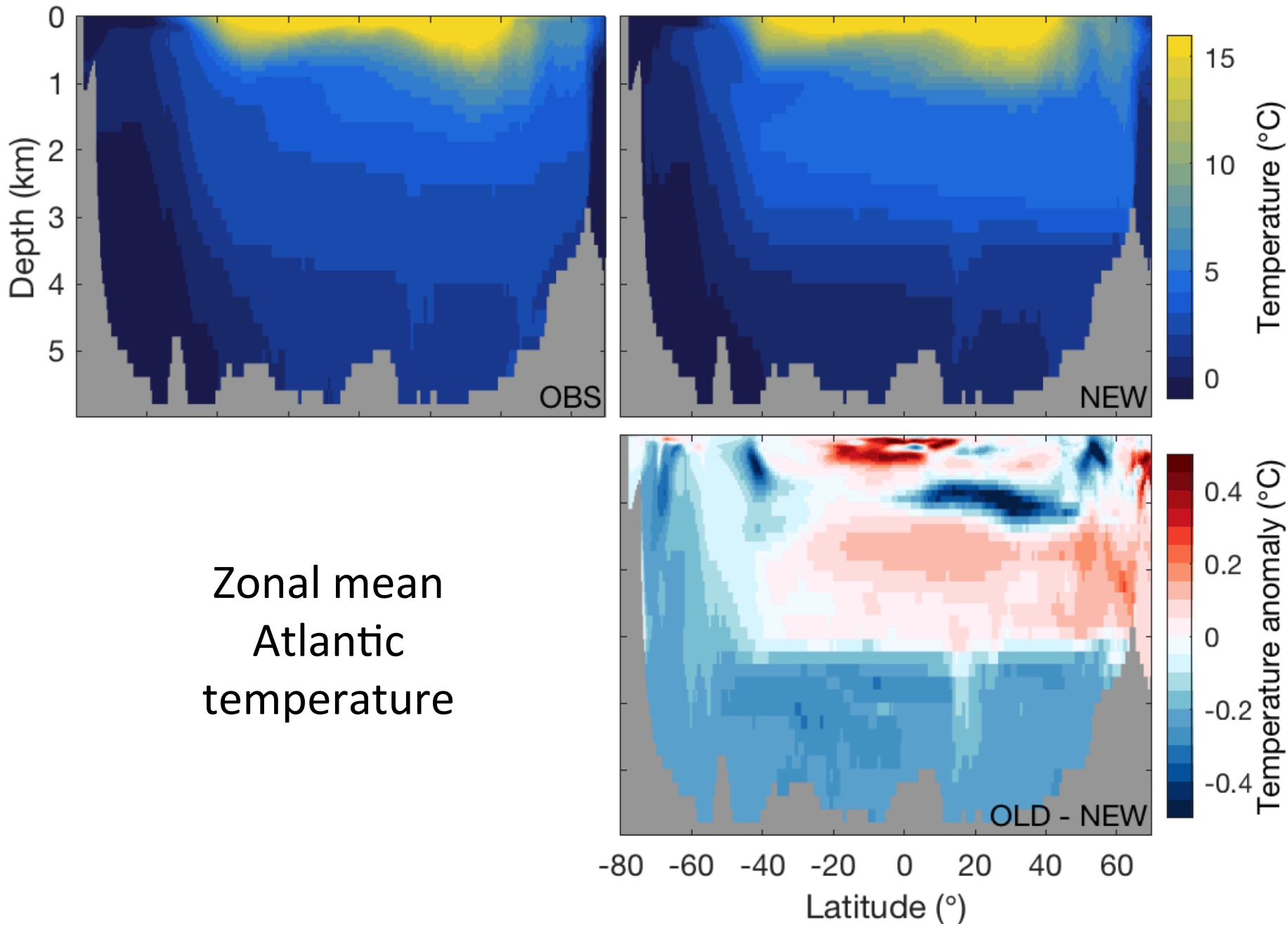
# Diffusivity distribution

## New scheme

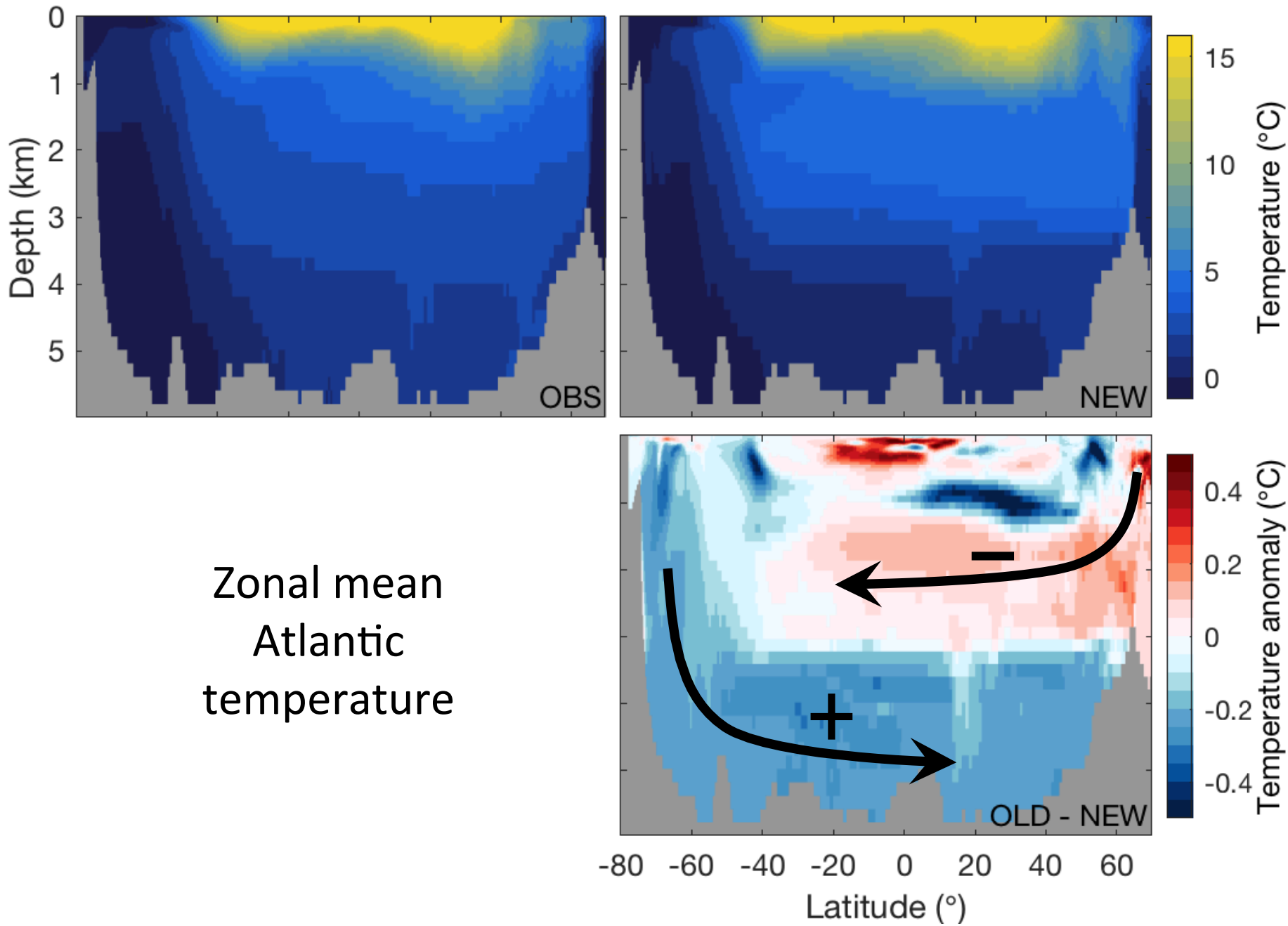
## Old scheme



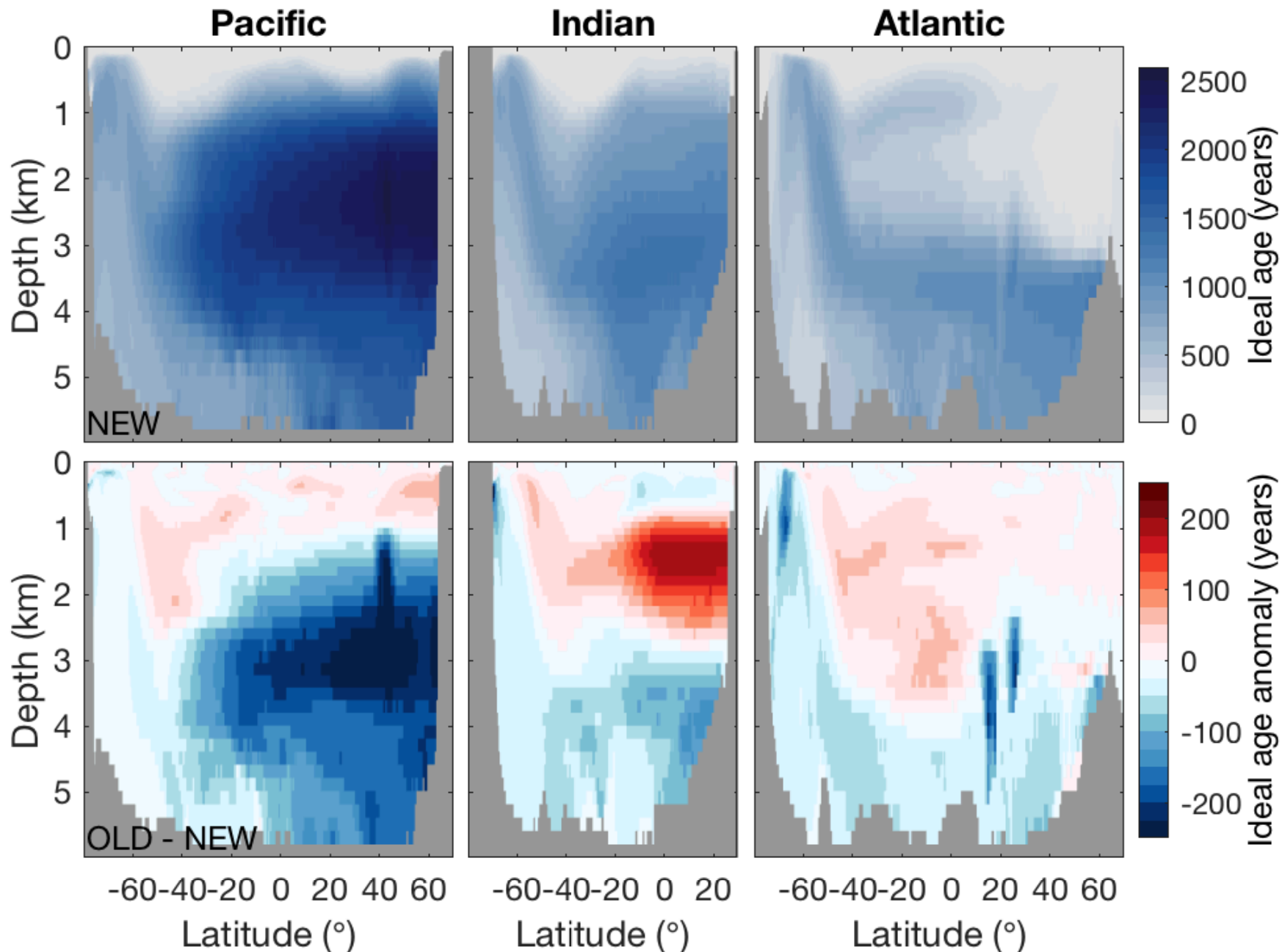
# Impact in NEMO 1° global ocean model



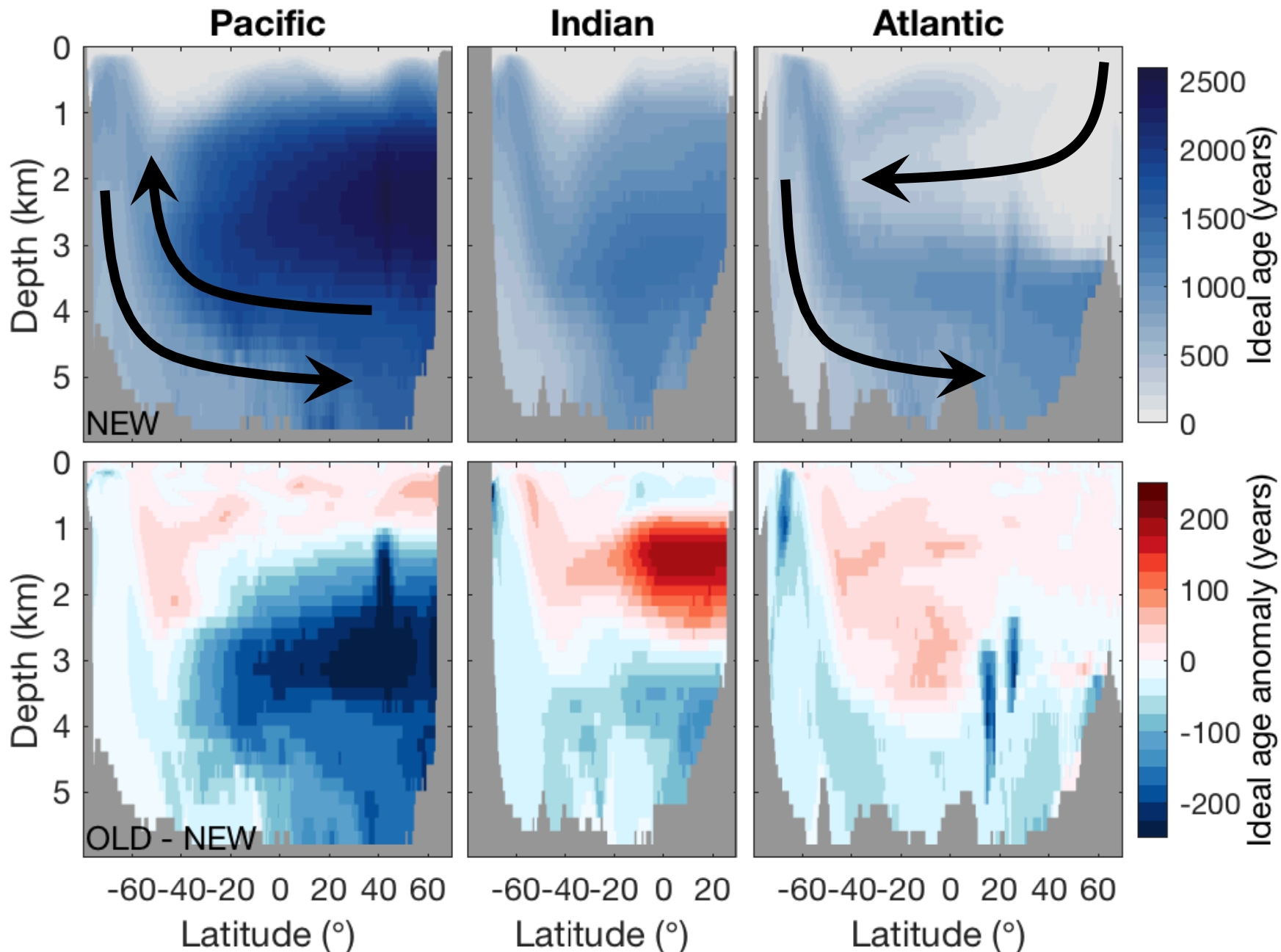
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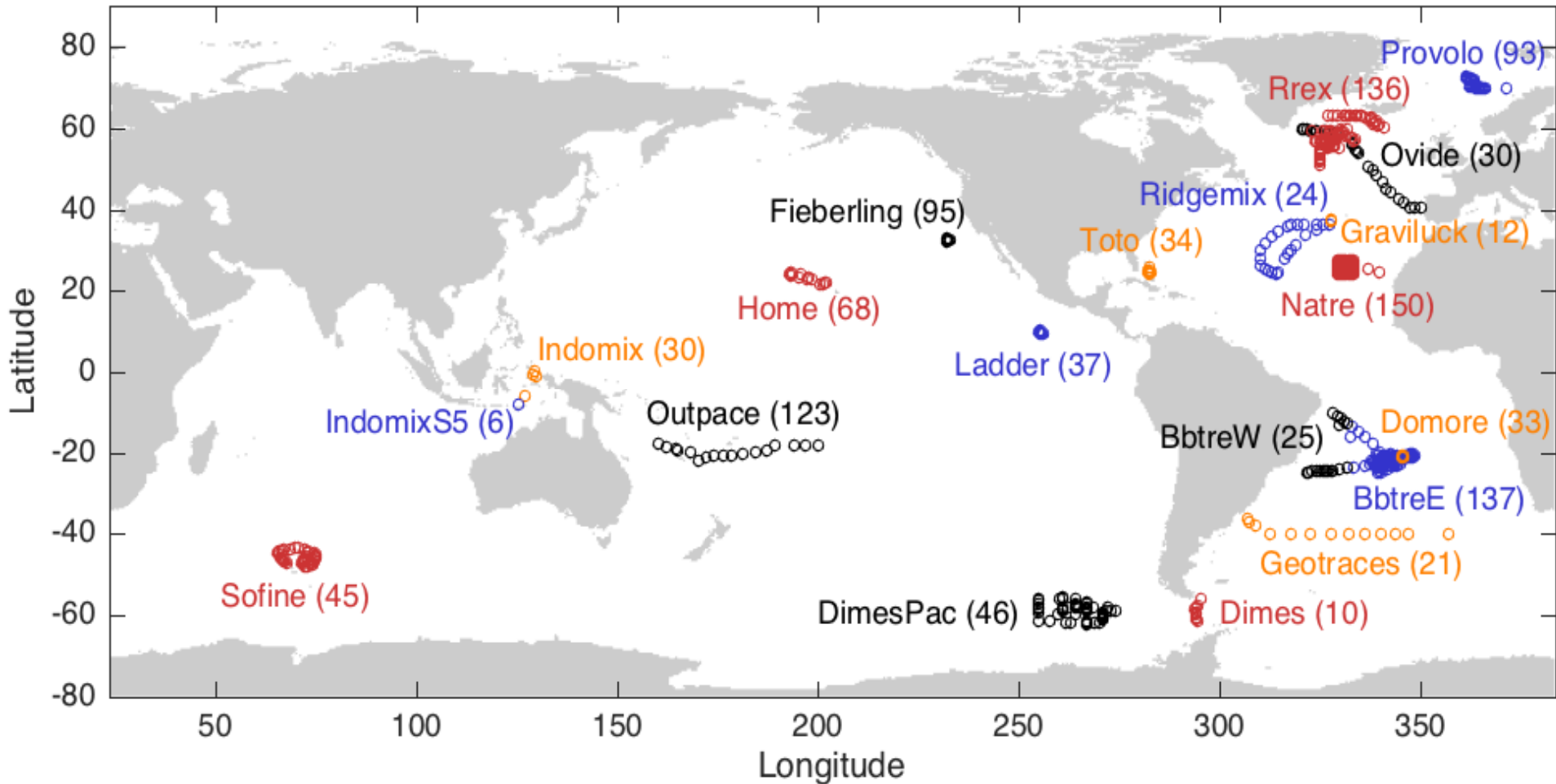
# Impact in NEMO 1° global ocean model



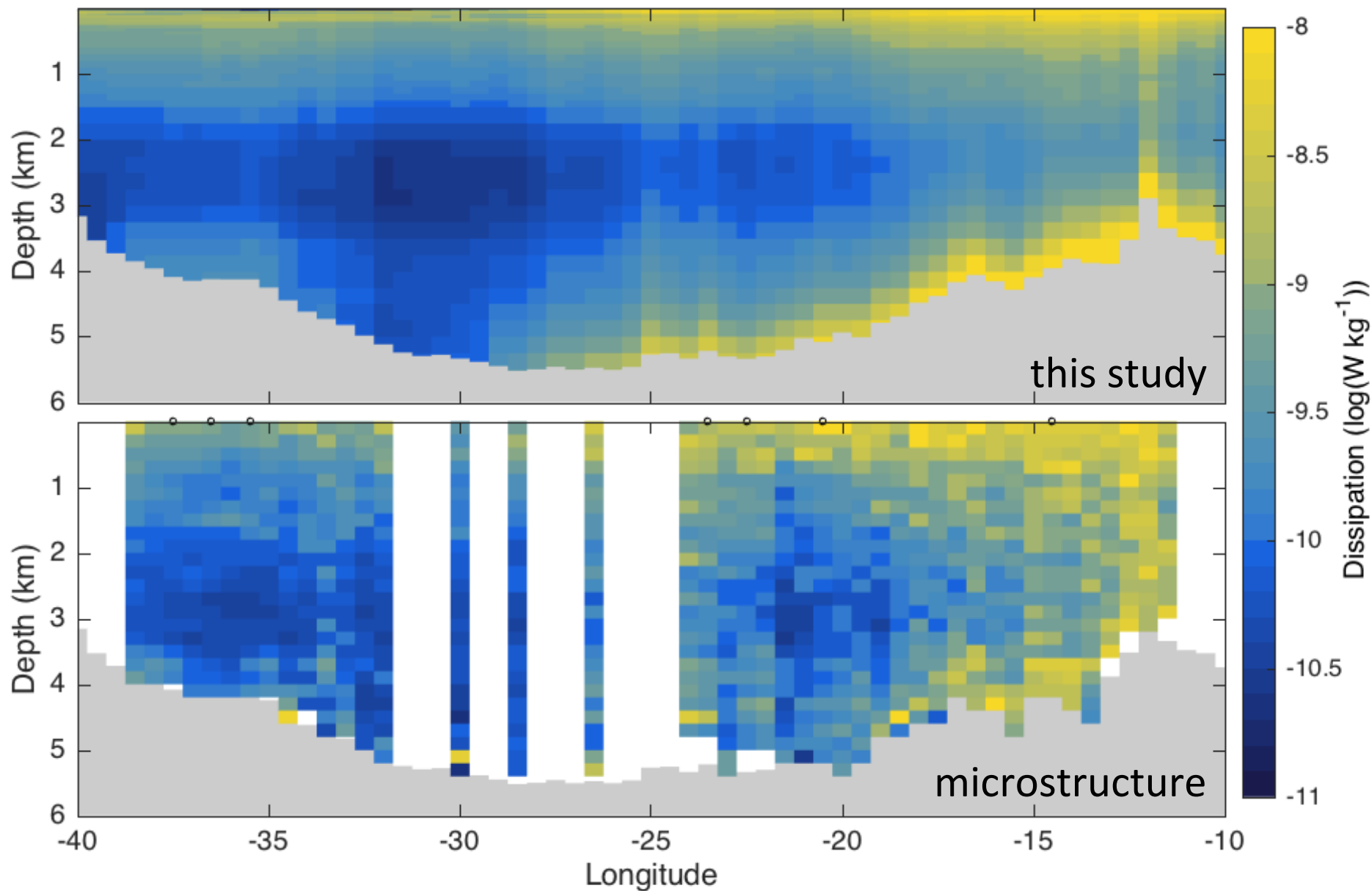


# Comparison with microstructure data

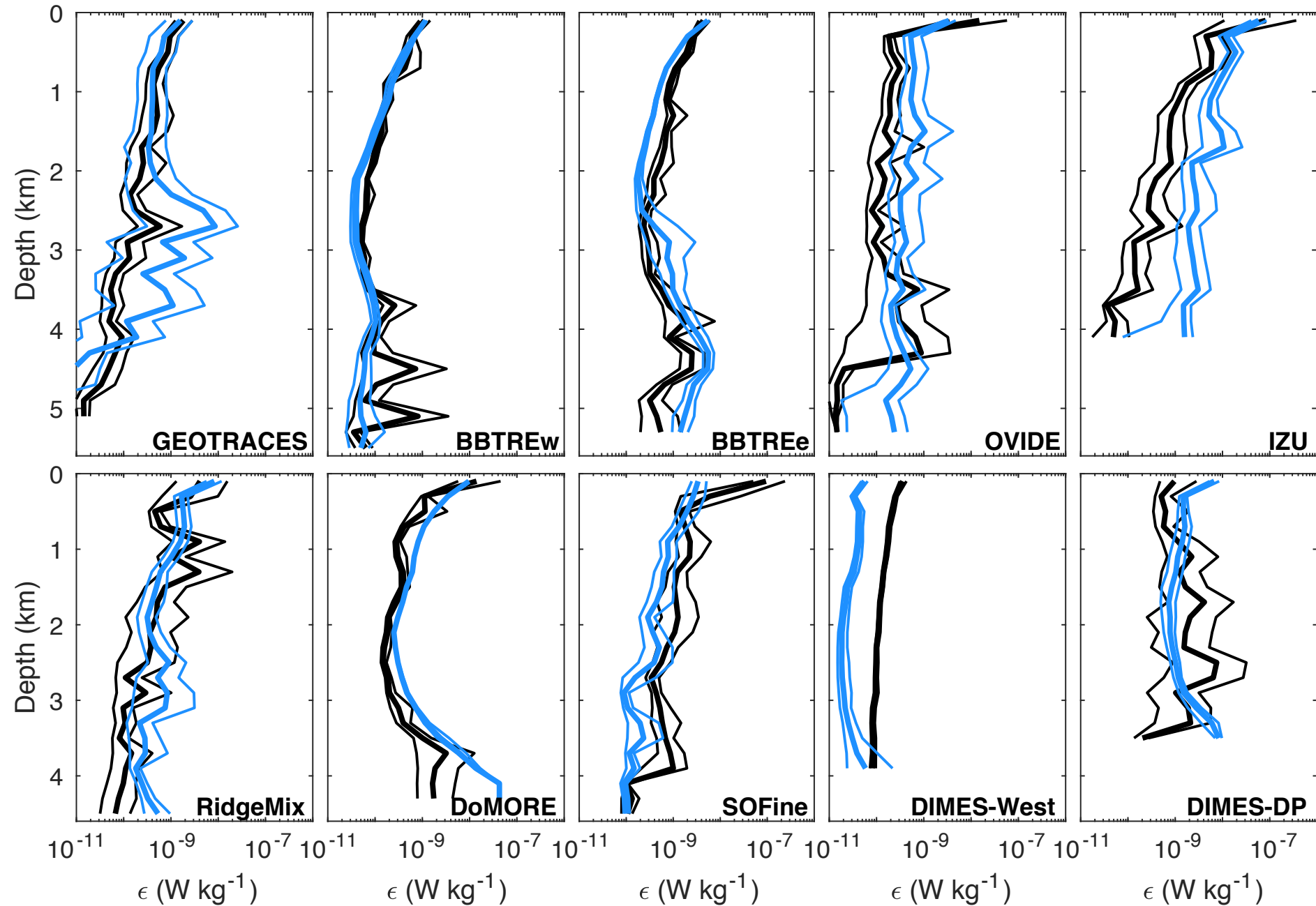
18 projects, 1155 profiles



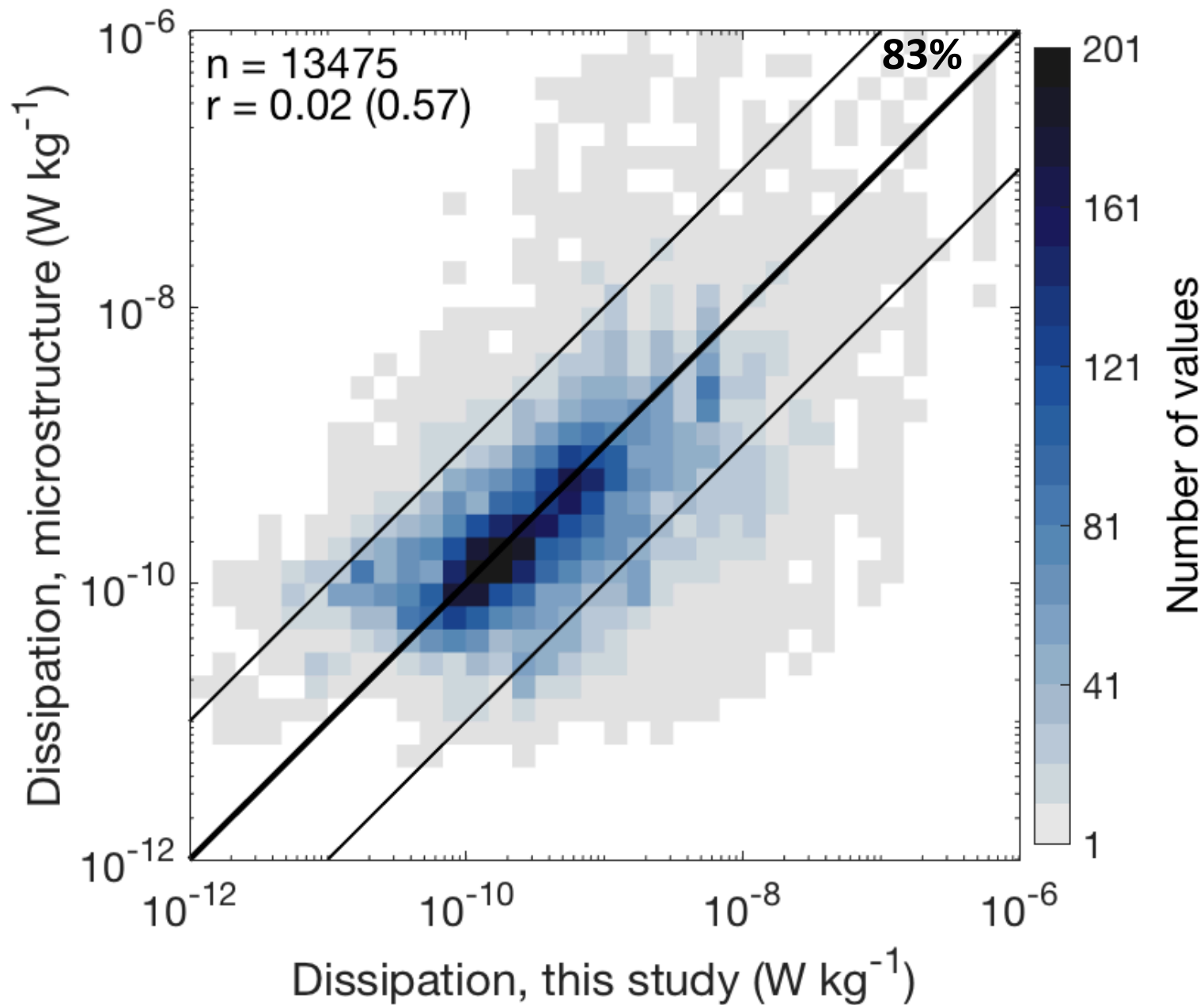
# Comparison with microstructure: Brazil Basin



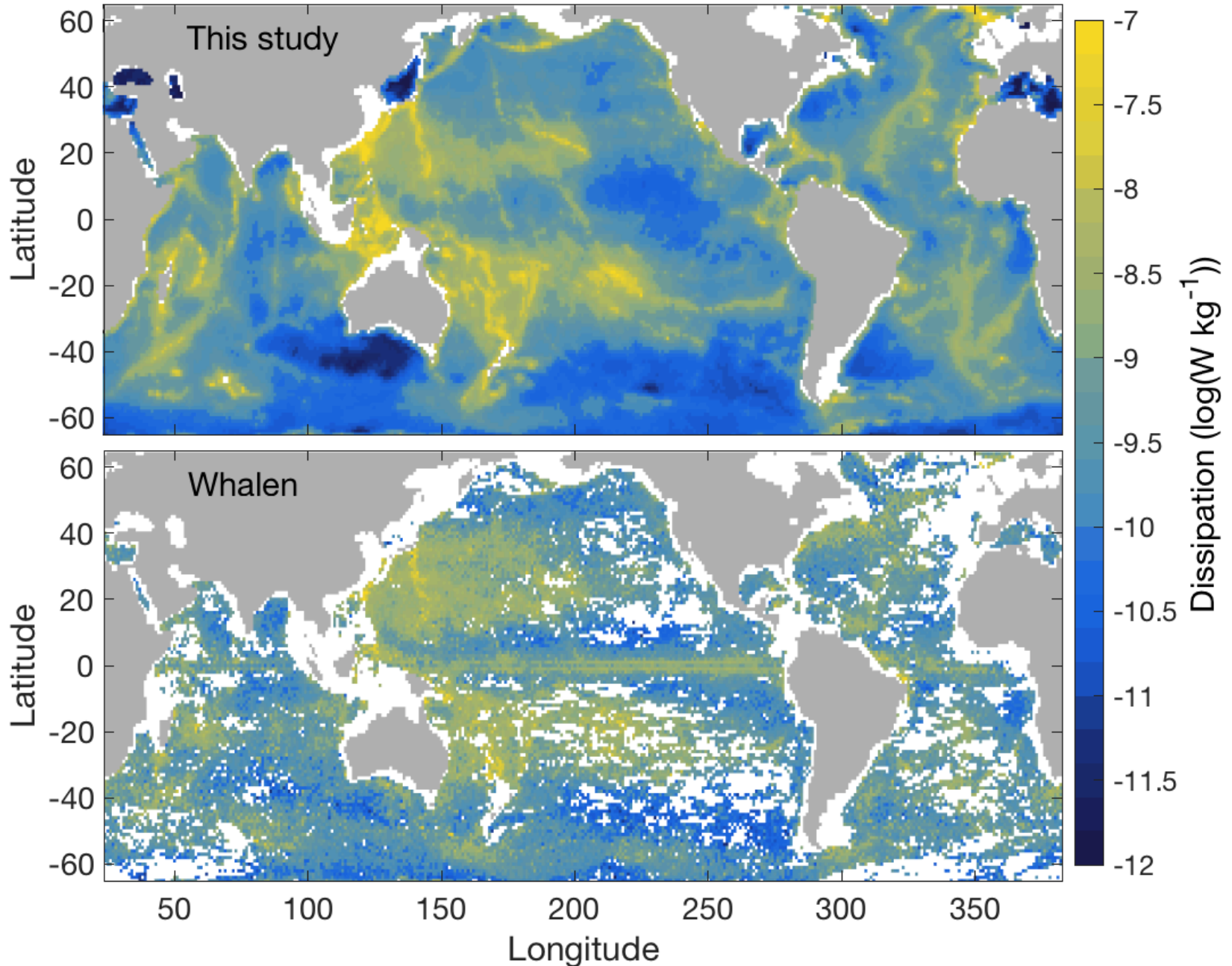
# Comparison with microstructure: profiles



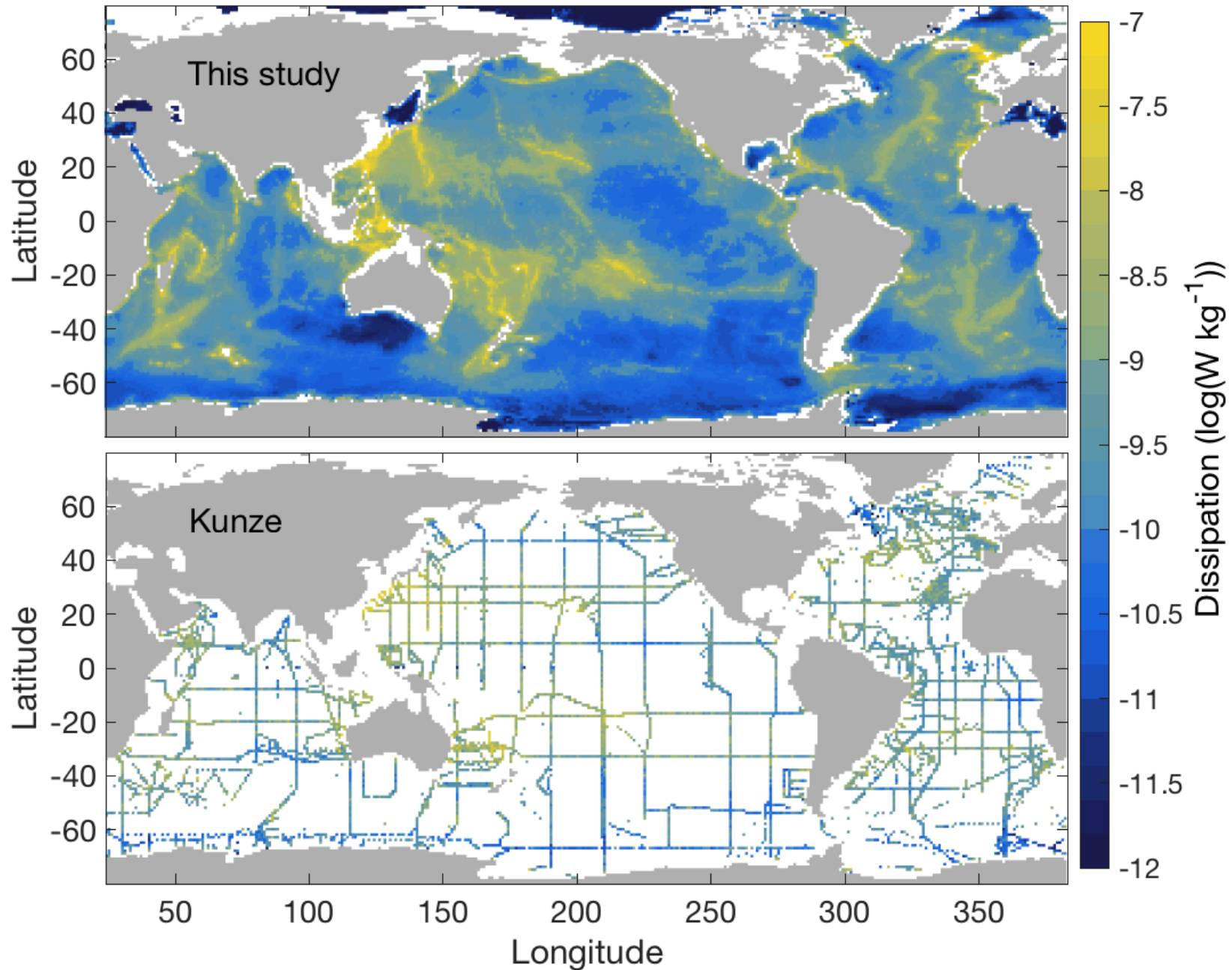
# Comparison with microstructure: scatter



# Comparison with finestructure (Argo)



# Comparison with finestructure (ship)



# Comparison with finestructure

**Kunze (ship)**

**Whalen (Argo)**

Number of values

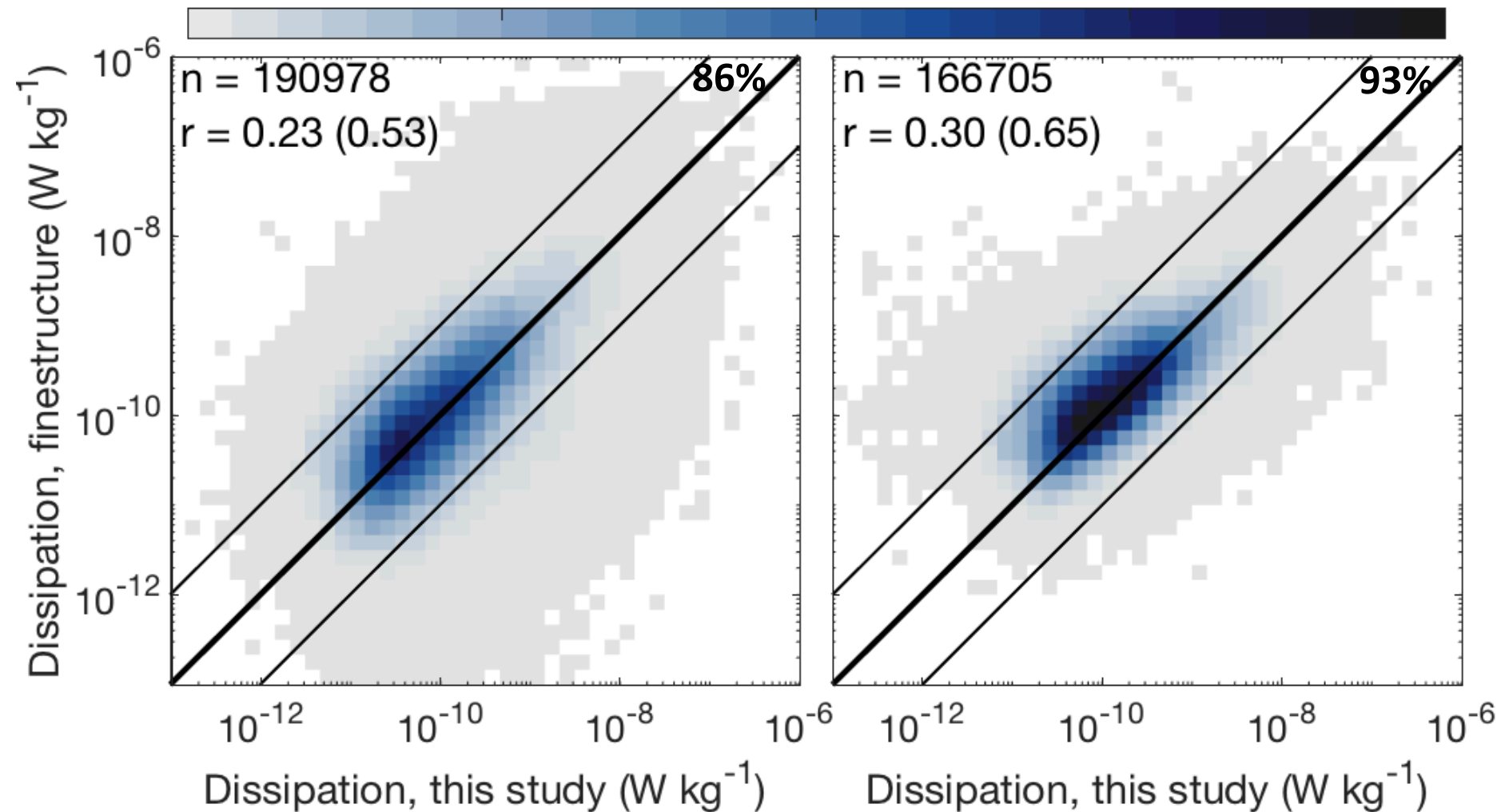
1

701

1401

2101

2801



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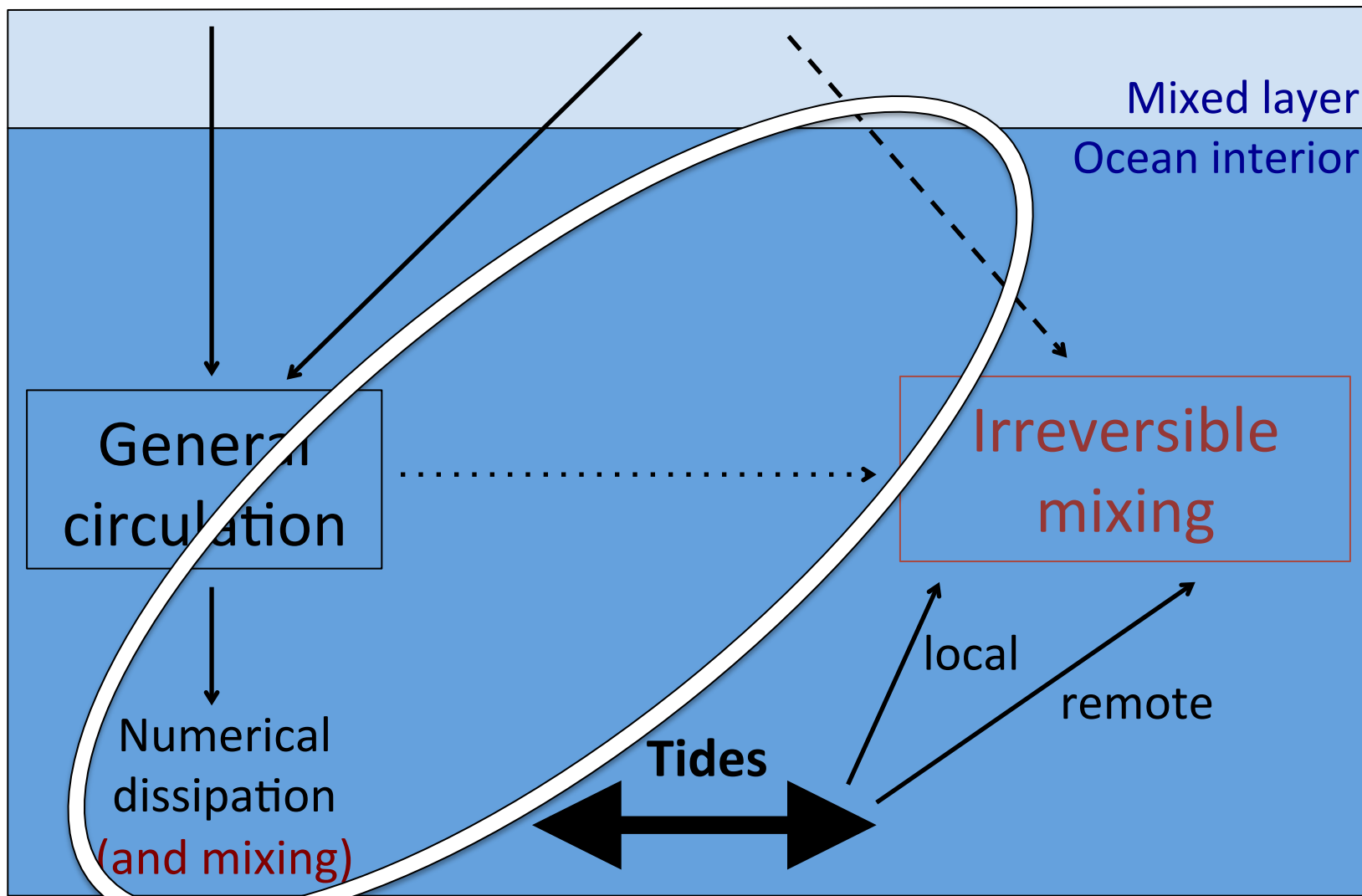


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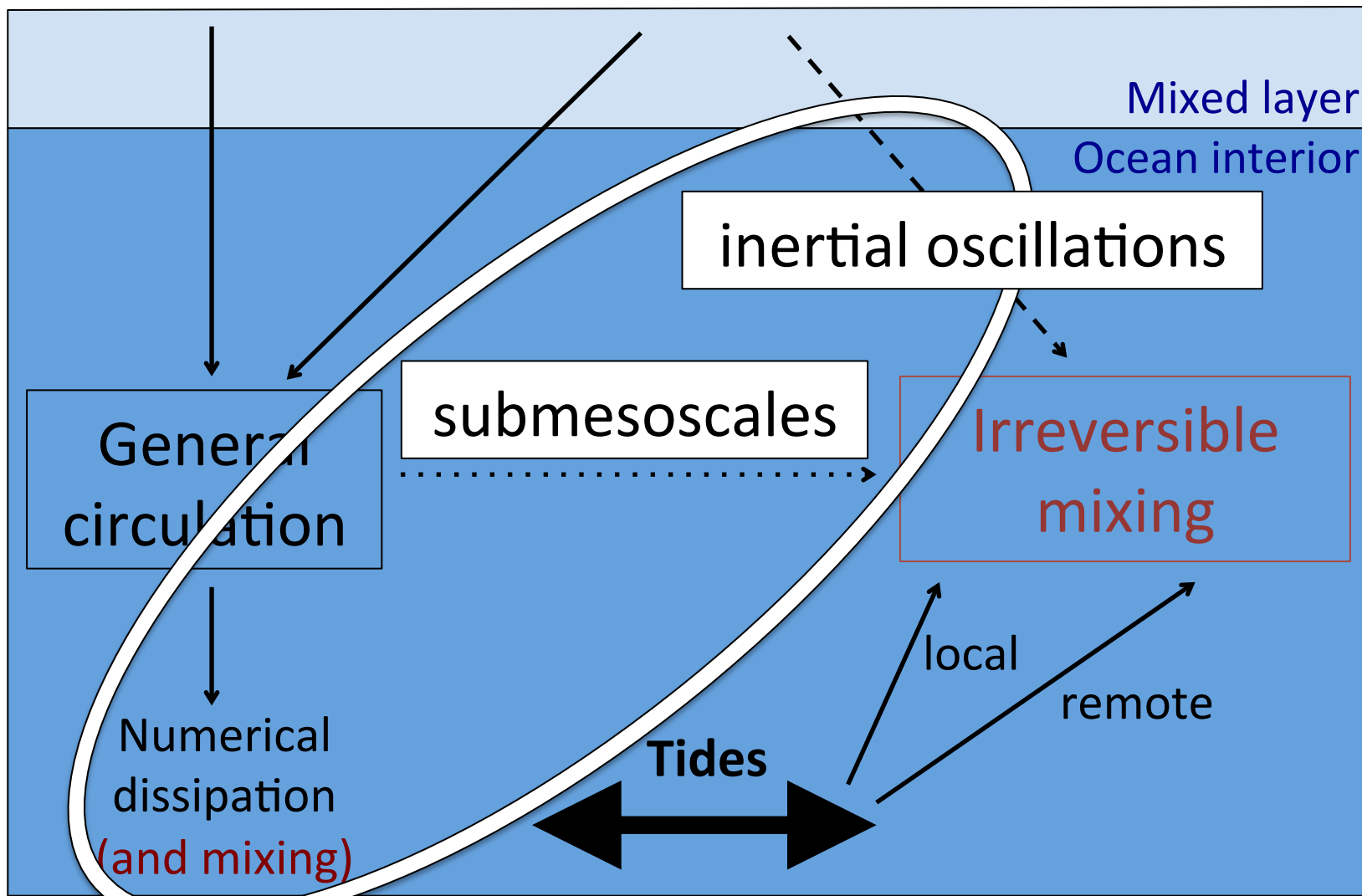


# Energy flows in ocean models

Surface buoyancy fluxes



Winds



Mixed layer

Ocean interior

inertial oscillations

General  
circulation

submesoscales

Irreversible  
mixing

Numerical  
dissipation  
(and mixing)

Tides

local

remote

# Wind-induced inertial oscillations

- Large source of mixing at base of mixed layer, weak source below.
  - Alford 2020: power into deep mixing  $\sim 0.1$  TW
- Ad hoc parameterizations exist for mixing near the base of the mixed layer:
  - Jochum et al. 2013: amplification of resolved shear in surface boundary layer module (resolution dependent)
  - NEMO: imposed vertical profile of TKE, function of surface TKE (not energy constrained)
- Challenge: parameterizations must be interactive with atmosphere ([online](#)).

# Submesoscale currents

- Submesoscale ( $< 20$  km) flows are abundant in the ocean interior.
  - Siegelman et al. 2020: energetic submesoscales in Southern Ocean interior down to 900 m
  - Naveira Garabato et al. 2019: submesoscale instabilities in bottom boundary currents
- Several effects (restratification, vertical mixing, isopycnal mixing) that might require separate parameterizations.
- No parameterization available for OGCMs yet, except for restratification by mixed-layer eddies (Fox-Kemper et al. 2008).

# Numerical mixing

- Progress in mapping and understanding spurious mixing due to discretization of advection.
  - Holmes et al. 2021: spurious mixing depends on resolution, viscosity, explicit mixing
- Adaptive vertical coordinates and improved advection schemes are promising pathways to reduce spurious mixing.
  - Griffies et al. 2020: Lagrangian-remap coordinate
- Many models still have large amounts of numerical mixing that can exceed the explicit mixing in the ocean interior.

# Conclusion

Surface buoyancy fluxes



Winds

